

**The Standard Model: “Is That All There Is?”**  
**(Emphasis on The Role of Precision)**

**Student Lecture**

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## **Michelson (The Master of Precision) 1894**

“The more important fundamental laws and facts of Physical Science have all been discovered, and these are now so firmly established that the possibility of their ever being supplanted in consequence of new discoveries is exceedingly remote... Our future discoveries must be looked for in the sixth place of decimals.”

Radioactivity **1896**

Electron Discovery **1897**

Special Relativity

General Relativity

Quantum Mechanics; Spin

**\*Dirac Equation 1928** (QM + S. Relativity + Spin + EM)

QED  $U(1)_{em}$  Photon ...

**Today**  $c = 299\,792\,458 \text{ m s}^{-1}$  **Exactly** (Meter Definition)

Natural Units  $c=1$  used in this talk

## Later

**Yang-Mills Non-Abelian Gauge Theories 1954**

**Standard  $SU(3)_C \times SU(2)_L \times U(1)_Y$  Model ~1967-1973**

**12 spin 1 bosons: 8 massless gluons;  $W^\pm, Z, \gamma$**

**3 generations of quarks and leptons**

**$e, \nu_e, u, d$     $\mu, \nu_\mu, c, s$     $\tau, \nu_\tau, t, b$  ( $m_t/m_\nu > 10^{13}!!$ ) (spin  $1/2$ )**

**Higgs Scalar Doublet:  $S^\pm, S^0, H$  source of mass (spin 0)**

**2012 Higgs (125GeV) Scalar Discovered at CERN!**

**Remnant of Electroweak Symmetry Breaking**

**Entering a New Age of Precision Higgs Physics!**

**2015:  $m_H = 125.09 \pm 0.24 \text{ GeV} ! \dots$**

## *Electroweak Unification History*

1957 - Parity Violation in Weak Interactions (Maximal!)

Lee & Yang Why is nature left-handed (Chiral)?

Following up on the work of his advisor (J. Schwinger)

**1961 Glashow  $SU(2)_L \times U(1)_Y$  Gauge Symmetry**

$W^\pm$ ,  $Z$  (massive) &  $\gamma$  (massless) gauge bosons

**(chiral) fermions massless left-right asymmetric**

All masses put in by hand

Explicitly Break Symmetry

$\gamma$ - $Z$  weak mixing angle introduced  $\sin^2\theta_W = (e/g)^2$

**Weak Neutral Currents (Z Interactions) Alluded To**

*Largely Ignored*

## 1967 Weinberg Introduces Higgs Mechanism

- Weinberg (following the work of P. Higgs) adds a scalar  $SU(2)_L$  doublet  $(\phi^+, \phi^0)$  with tachyonic mass to the model that breaks  $SU(2)_L \times U(1)_Y \rightarrow U(1)_{em}$  at the vacuum level
- $\langle \phi \rangle \approx 250 \text{ GeV}$  gives masses to  $W^\pm$ ,  $Z$  and all fermions  
 $\sin^2 \theta_w^0 = 1 - (m_W^0 / m_Z^0)^2 = (e^0 / g^0)^2$  Natural Relations...  
Predicts weak neutral currents... & Higgs Boson  
1971 Renormalizability proved by 'tHooft

Is the Higgs Mechanism Fundamental or Dynamical?

Is there just a single Higgs doublet? Several?

$H=0^{++}$  Remnant Predicted – Higgs Boson, Others  $h$ ,  $A$ ,  $H^\pm$ ...

*H coupling to particles proportional to their masses*

*$W$ ,  $Z$ ,  $t$ ,  $b$  large...  $e$ ,  $u$ ,  $d$  very small (detectable?)*

## Higgs (125GeV) Discovery & Properties

- ATLAS and CMS Experiments have strong evidence for a
- Higgs like (spin 0) new particle with mass 125GeV

### Expected Higgs SM Properties

<i>H</i> Decay Channel	Branching Ratio
$b\bar{b}$	0.578
$WW^*$	0.215
$gg$	0.086
$\tau^+\tau^-$	0.063
$c\bar{c}$	0.029
$ZZ^*$	0.026
$\gamma\gamma$	$2.3 \times 10^{-3}$
$Z\gamma$	$1.5 \times 10^{-3}$
$H \rightarrow ZZ^* \rightarrow l_1^+ l_1^- l_2^+ l_2^-$	$1.2 \times 10^{-4}$
$H \rightarrow ZZ^* \rightarrow l^+ l^- \nu \bar{\nu}$	$3.6 \times 10^{-4}$

## Some Important Precision EW Parameters Tied Together by Natural Relationships

<u>Quantity</u>	<u>2008 Value</u>	<u>2015 Value</u>	<u>Comment</u>
$\alpha^{-1}$	137.035999084(51)	<b>137.035999049(90)</b>	$\alpha^{-1}(a_e)$ vs $\alpha^{-1}(\text{Rb})$
$G_\mu$	$1.16637(1) \times 10^{-5} \text{GeV}^{-2}$	<b><math>1.1663787(6) \times 10^{-5} \text{GeV}^{-2}</math></b>	$\tau_{\mu^+}$ PSI
$m_Z$	91.1875(21) GeV	91.1876(21) GeV	-
* $m_t$	171.4(2.1) GeV →	<b><u>173.3(0.8) GeV</u></b>	FNAL/LHC
* $m_H$	>114 GeV →	<b><u>125.09(0.24) GeV</u></b>	
$m_W$	80.410(32) GeV →	<b><u>80.385(15) GeV</u></b>	LEP2/FNAL
$\sin^2\theta_W(m_Z)_{\text{ave}}$	0.23125(16)	0.23125(16)	Z Pole Ave.

### Best individual Z pole determinations:

$\sin^2\theta_W(m_Z)$	0.23070(26)	0.23070(26)	SLAC $A_{LR}$
$\sin^2\theta_W(m_Z)$	0.23193(29)	0.23193(29)	CERN $A_{FB}(bb)$

**(3 sigma difference?)**

## A *Beautiful* Electroweak Relation

$SU(2)_L \times U(1)_Y$  + Higgs Doublets + Renormalizability

- $\sin^2 \theta^0_W = 1 - (m^0_W / m^0_Z)^2 = (e^0 / g^0)^2$  Natural Bare Relation

Radiative (Loop) Corrections - Finite & Calculable!

Demonstrated by Bollini, Giambiagi & Sirlin (1972)

WJM(1974) Thesis: Finite Parts Calculated

Main effect:  $\alpha = 1/137 \rightarrow \alpha(m_Z) \sim 1/128$  Large 7% VP

Later: Large  $\alpha m_t^2 / m_W^2$  Corrections M. Veltman

Higgs loop corrections smaller but not negligible



# Standard Model Predictions Through 2 loops

*Assuming No New Physics*

$$\sin^2 2\theta_W(m_Z)_{MS} = 2\sqrt{2}\pi\alpha/m_Z^2 G_\mu (1 - \Delta r'(m_t, m_H)) \quad m_H = 125 \text{ GeV!}$$

$$\Delta r'(m_t, m_H) = 0.0598(2) \rightarrow \sin^2 \theta_W(m_Z)_{MS} = \underline{0.23124(6)} \pm 0.03\%$$

Currently  $\sin^2 \theta_W(m_Z)_{ave} = 0.23125(16)$  Excellent Agreement

Error Expected to be reduced (improved  $m_t$ ) to  $\sim \pm 0.01\%$

$$m_W^2 = \pi\alpha/\sqrt{2} G_\mu \sin^2 \theta_W(m_Z)_{MS} (1 - \Delta r(m_Z)_{MS})$$

$$\Delta r(m_Z)_{MS} = 0.0693(2) \rightarrow m_W = 80.362(6)$$

Currently  $m_W^{\text{exp}} = \underline{80.385(15) \text{ GeV}}$  1.4 sigma high

Any significant difference between SM prediction  
and Experiment Implies “New Physics” (No Signal Yet!)

The Higgs appears to be a fundamental remnant of EW symmetry breaking and mass generation. It completes the Standard  $SU(3)_C \times SU(2)_L \times U(1)_Y$  Model spectrum.

One can ask:

***Is that all there is?***

Examples of possible additional “New Physics”:  
Supersymmetry, Other Scalars, Heavy Quarks or Leptons, Dark Particles ... Additional Gauge Interactions  
...

***Or is the Higgs the last hurrah of Particle Physics!***

Look for deviations in the 4th-6th decimal places!

(from Brian Malow)

- **"Higgs boson walks into a church, and the priest says, 'I'm sorry we don't allow Higgs bosons to come to churches.' And [the Higgs] says, 'But without me, you can't have mass.'"**

# *The Roots of Precision* *Quantum Electrodynamics (QED)*

## 1.) *Historical Introduction*

- i) Wolfgang Pauli (**1924 Exclusion Principle!**)
- ii) Spin (1925) *A Great but clouded discovery*
- iii) The Dirac Equation (1928)  $g_e=2$  & **Antiparticles!**
- iv)  $U(1)_{em}$  Local Gauge Invariance

## 2.) *Post WWII Developments (1947-48)*

### *The Birth of Quantum Electrodynamics (QED)*

- i) Electron Anomalous Magnetic Moment  $g_e-2$
- ii) Lamb Shift: Hydrogen  $2S_{1/2}-2P_{1/2}$
- iii) The Muon: “Who ordered that?”  $m_\mu \approx 207m_e$

### 3.) **More Recent Developments**

i)  $g_e-2$  (5 loops!)

ii) Lamb Shift?

iii)  $g_\mu-2$  (New Physics - Supersymmetry/Something Else?)

### 4.) **“Light” Dark Photon (Dark Matter Force Mediator)**

**Viewer Discretion Advised** - Speculative

### 5.) **Muonic Hydrogen Lamb Shift**

**The Proton Size Puzzle** ( $r_p(ep)$  vs  $r_p(\mu p)$  atom)

**8 sigma difference**

### 6.) **Outlook**

## 1.) Historical Introduction

1897 Electron ( $e^-$ ) Discovered J.J. Thomson  
The Start of Elementary Particle Physics

Early 20<sup>th</sup> Century

Quantum Mechanics ( $\gamma$  photon)

Special & General Relativity

1919 Proton ( $p^+$ ) Discovered  $m_p \approx 1840 m_e$  Ernest Rutherford

1931 Neutron (n) Discovered by Chadwick

1926 Schrodinger Equation – Non-Relativistic QM

In a 1924 letter to Lande, W. Pauli presented his now famous  
**“Pauli Exclusion Principle”**

Atomic Spectroscopy of the Bohr Atom, electrons  
classified by quantum no.:  $n$ ,  $l$ ,  $m$  &  $t$ =**twofoldness**

**No two electrons can have identical quantum numbers!**

Fundamental Property of Nature → Explained Chemistry!

***But, what was “twofoldness”?***

# Wolfgang Pauli

Pauli Portraits

6/1/11 11:41 AM

## Wolfgang Pauli





ii) **Electron Spin (1925)**  
**Nobel Prize?**

In 1925, Kronig (unpublished) and independently Uhlenbeck and Goudsmit interpret “twofoldness” as Electron spin  $S=\pm\frac{1}{2}$ . Wavefunction antisymmetric under Interchange of electrons.

**Pauli:** *“A clever idea but nothing to do with nature!”*

Eventually spin established (Thomas relativistic factor of 2)

Electron magnetic moment  $\mu_e = g_e e/2m_e \mathbf{S}$

**$g_e = \text{gyromagnetic ratio} = 2$**

**Ironic:** Pauli 2x2 **spin** matrices (Non-relativistic)

iii) **The Dirac Equation** (1928)  $g_e=2$

*“The Dirac equation like youth is often wasted on the young”*

**The Stage in 1928**

Non Relativistic Schroedinger Eq. First Order

Relativistic Klein-Gordon Scalar Eq. (spin 0) Second Order

Spin 1/2 - Pauli 2x2 Matrices (non-relativistic spin)

**The Genius of Dirac**

QM+Special Rel.+Spin+EM Gauge Invariance  $U(1)_{em}$

First Order Equation Spinor (4 Component)

$$i(\partial_\mu - ieA_\mu(\mathbf{x}))\gamma^\mu\psi(\mathbf{x}) = m_e\psi(\mathbf{x}),$$

4x4  $\gamma^\mu$  (Dirac) matrices:  $\gamma^\mu\gamma^\nu + \gamma^\nu\gamma^\mu = 2g^{\mu\nu}I$

**Similar eq. for the proton  $m_p \approx 1840m_e$**

Mag. Moment:  $\boldsymbol{\mu} = g_e e/2m_e \mathbf{s}$   $g_e = \underline{2}$  (Not 1!)

As Observed Experimentally

## Automatic Unexpected Success of Dirac Eq.

### Dirac Derivation of $g_e = 2$ (1928 & “QM” Book)

Go to second order formalism (apply

$$[-i(\partial_\mu - ieA_\mu(\mathbf{x}))\gamma^\mu - m_e] \times [i(\partial_\mu - ieA_\mu(\mathbf{x}))\gamma^\mu - m_e]\psi(\mathbf{x})$$

and find terms in Klein-Gordon Eq.

$$\boldsymbol{\mu} \cdot \mathbf{H} + i\rho_1 \boldsymbol{\mu} \cdot \mathbf{E} \text{ (edm?) } \boldsymbol{\mu} = \underline{2}e/2m_e \mathbf{s}$$

Imaginary Part? - **Non Physical?** → Ignore?

By the 4th edition of “QM” he got rid of it

(What is an electric dipole moment (edm)?

and what is a chiral phase?)

**Later realized Negative Energy Solutions!**  
**(Dirac Equation largely ignored or even ridiculed)**

**W. Pauli was a primary antagonist**

***Dirac predicts positron, antiproton, antihydrogen...***

***Antimatter Discovery Dirac's crowning glory!***

***Doubled Particle Spectrum!***

**Why is the Universe Matter-Antimatter Asymmetric?**

**Baryogenesis! (Sakharov Conditions)**

**(1964-CP Violation Discovered-CKM Not Enough)**

**"New Physics" Source of CP Violation Needed!**

**Supersymmetry, 4th Generation, Multi-Higgs...**

**Baryogenesis:  $N_B/N_\gamma \approx 10^{-10}$**

**1957 - Parity Violation in Weak Interactions (Maximal!)**

**Lee & Yang Why is nature left-handed (Chiral)?**

**1964- CP Violation Discovered in Kaon Decays**

**1967 Sakharov Conditions:**

- 1) Baryon Number Violation**
- 2) CP Violation (strong source)**
- 3) Non-Equilibrium 1<sup>st</sup> Order Phase Transition**

## Completing the Picture?

1930 Pauli Proposes the Neutrino ( $\nu$ ) (weak interactions)

1931 Neutron ( $n$ ) Discovered (strong interactions)

1932 Positron ( $e^+$ ) Discovered (***Anti-Matter Exists!***)

- 
- 
- 

**p, n, e,  $\nu$  basic ingredients of our Universe (Existence)**  
**strong, weak, electromagnetic & gravitational interactions**

***Is that all there is?***

# Today

Elementary Particle Physics *(Many Particles!)*

$SU(3)_C \times SU(2)_L \times U(1)_Y$  Standard Model

8 gluons +  $W^\pm, Z, \gamma$  ***gauge bosons (spin 1)***

3 generations of ***quarks & leptons (mix->CP violation)***

***e,  $\nu_e, u, d$     $\mu, \nu_\mu, c, s$     $\tau, \nu_\tau, t, b$  ( $m_t/m_\nu > 10^{13}!!$ ) (spin  $1/2$ )***

Complex Scalar Doublet:  $S^\pm, S^0, H$  source of mass ***(spin 0)***

***Now (2012) Complete! Higgs (H) Boson Discovery***

***Remnant of Particle Mass Origin***

What Else Is There? New Particles? Interactions?

***Supersymmetry (Doubles The Spectrum!)***

***Weakly Coupled Hidden Sector?***

***So far: No direct evidence for Supersymmetry,  
At The LHC (Large Hadron Collider)!***  
***Still Early – Nevertheless some tension***

***The Higgs –May Be Last Particle Ever Discovered?***  
***(Probably Not)***

Left with Mysteries: Why Baryogenesis? CP?  
Why 3 Generations?  
Why Parity Violation?  
Dark Matter, Energy...



## We could add extra terms to the Dirac Equation

(using  $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$ )

$$e/4m_e a_e F_{\mu\nu}(x) \sigma^{\mu\nu} \psi(x) + i/2d_e \gamma_5 F_{\mu\nu}(x) \sigma^{\mu\nu} \psi(x)$$

Anomalous Mag. Mom.

$$g_e = 2(1 + a_e)$$

$a_e =$  Pauli Term

Electric Dipole Mom.

Violates P&T (CP)

Not Observed

$$d_e < 10^{-28} \text{e-cm}$$

But Must Exist!

Pauli opposed the Dirac Equation (Neg Energy Sol.)

Later became so converted that he opposed proton

Mag. Moment exp. "It must be  $g_p e/2m_p \mathbf{s}$   $g_p = 2!$ "

***Experiment  $g_p = 5.59$***

## iv) $U(1)_{em}$ Local Gauge Invariance

Electrodynamics (with charged electron source)

Invariant under local  $U(1)_{em}$  gauge transformations

$$L = \frac{1}{4}F_{\mu\nu}(x)F^{\mu\nu}(x) + \psi^*(x) \gamma^0 \{i(\partial_\mu - ieA_\mu(x))\gamma^\mu - m_e\} \psi(x)$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

$$A_\mu(x) \rightarrow A_\mu(x) - ie\partial_\mu \Lambda(x) \quad \psi(x) \rightarrow \exp(ie\Lambda(x))\psi(x)$$

**Generalization of Charge Conservation**

**Fundamental principle of interactions**

**Equations of motion: Maxwell's Eqs & Dirac Eq.**

## 2.) Post WWII Developments (1947-48)

### 1947 Small Anomalous Atomic Fine Structure Effects

G. Breit: maybe  $a_e = (g_e - 2)/2 \neq 0$

### 1948 Schwinger Calculates: $a_e = \alpha/2\pi \approx \underline{0.00116}$ ( $\alpha = e^2/4\pi = 1/137$ )

Agreed with measurement of Kusch & Foley!

**Great Success of QED -Quantum Field Theory**

### 1947 Lamb measures the $2P_{1/2}$ - $2S_{1/2}$ splitting

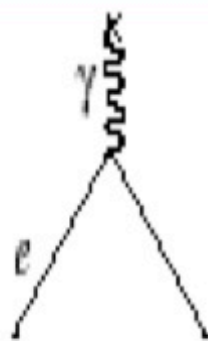
vacuum polarization, electron self-interaction

***$a_e$  and Lamb shift start of QED (Quantum Electrodynamics)***

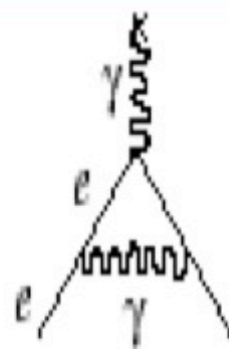
### 1947 Muon established $m_\mu \approx 207m_e$ “Who ordered that?”

Later  $\tau_\mu = 2.2 \times 10^{-6} \text{sec}$  very long very precise!

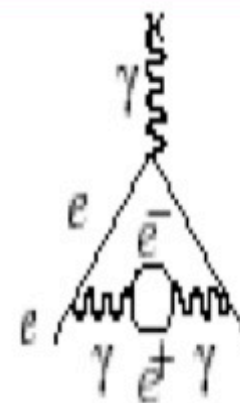
## Anomalous Magnetic Moment Contributions



Dirac



Schwinger



## **Basic Quantum Electrodynamics**

Quantize  $A_\mu(x)$  and  $\psi(x)$  fields  $\rightarrow$  operators

Represents interacting photons and electrons (positrons)

Parameters  $m_e^0$  and  $e_0$  bare electron mass and charge

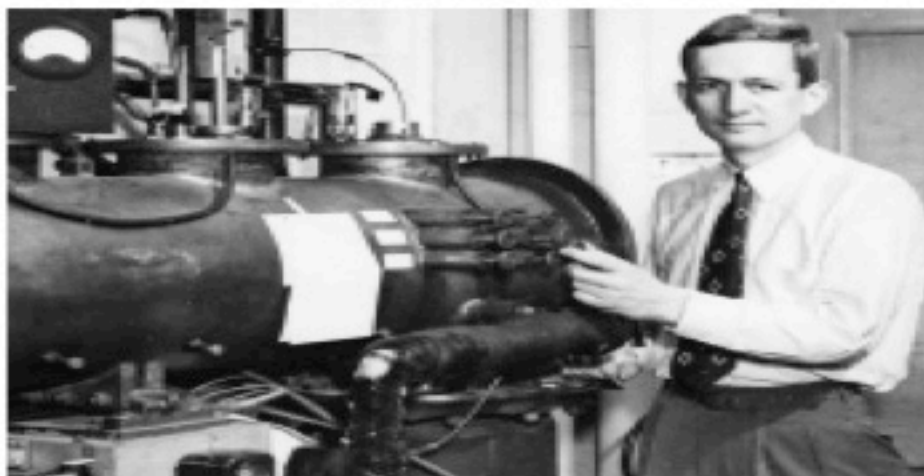
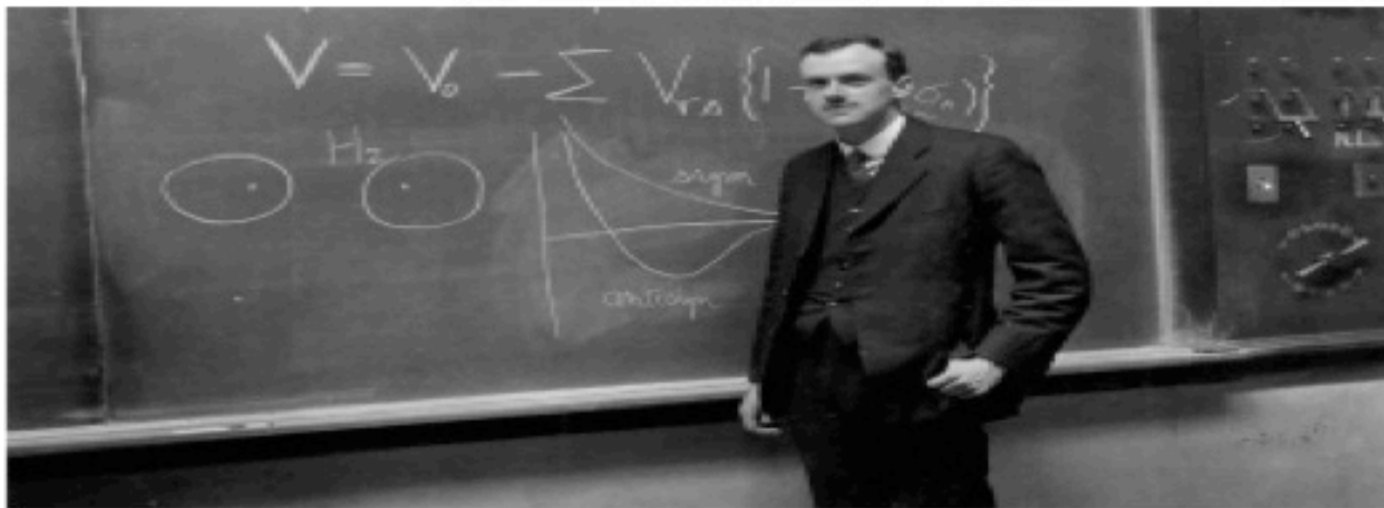
Renormalized to  $m_e$  and  $e$  physical mass and charge

Interaction strength  $e^2/4\pi \approx 1/137$  fine structure constant

Clockwise:

Julian Schwinger,  
Polykarp Kusch,  
Paul Dirac,  
Norman Ramsey and  
Edward Purcell

Courtesy AIP Emilio  
Segrè Visual Archives  
(full credits overleaf)





Mount Auburn Cemetery



## Anomalous Magnetic Moments Today

$$a_l = (g_l - 2)/2 \quad l = e, \mu$$

$$a_e(\text{exp}) = 0.00115965218073(28) \quad \text{unc. } \pm 28 \times 10^{-14}!$$

(Hanneke, Fogwell, Gabrielse: PRL 2008)

$$g_e = 2.00231930436146(56)$$

*Most precisely known dimensionless physical quantity!*

***Future Goal: factor  $\geq 4$  improvement?***

$$a_e(\text{SM}) = \alpha/2\pi - 0.328478444002546(\alpha/\pi)^2$$

$$+ 1.181234016(\alpha/\pi)^3 - 1.9097(20)(\alpha/\pi)^4$$

$$+ \underline{7.795(336)(\alpha/\pi)^5} \dots + 1.68(2) \times 10^{-12}(\text{had}) + 0.03 \times 10^{-12}(\text{EW})$$

Aoyama, Hayakawa, Kinoshita, & Nio 2012 & 2015 Updates!

Spectacular Computational Achievement

Uncertainty  $\pm 7 \times 10^{-14}$  (QED theory)  $\pm 2 \times 10^{-14}$  (Hadronic)



## **Alpha determination: Rydberg + $m_e/m_{Rb}$**

$$R_\infty = 1.0973731568527(73) \times 10^7 \text{m}^{-1}$$

$$\frac{1}{2}m_e\alpha^2 = 13.60569253(30)\text{eV}$$

$$\alpha^{-1}(^{87}\text{Rb}) = 137.035999049(90)?$$

*Bouchendira et al. PRL. (2011) factor 10 improvement!*

*Ongoing  $^{87}\text{Rb}$  exp. Goal - Another factor of 7 improvement!*

$$\Delta a_e = a_e(\text{exp}) - a_e(\text{theory}) = -0.91 (0.82) \times 10^{-12} \text{ Note Sign}$$

$$\text{Error Budget: } \pm 77 \times 10^{-14}(\text{alpha}) \pm 28 \times 10^{-14}(\text{exp.}) \pm 7 \times 10^{-14}(\text{th.})$$

### **Further Improvement in $\Delta a_e$**

*Factor 2.6 Sensitivity Improvement (better)  $\alpha^{-1}(^{87}\text{Rb})$*

*New  $a_e$  Experiment (4 x better)!*

**Very good for constraining long distance new physics (eg Dark Photon)**

## ii) Hydrogen Lamb Shift Update?

Depends on proton structure (size)  $r_p$  (radius)

***How large is the proton (rms) radius?***

About a Fermi (fm) =  $10^{-13}$ cm

$\langle r_p^2 \rangle = \lim_{Q^2 \rightarrow 0} -6 \frac{dF(Q^2)}{dQ^2}$  em form factor

**CODATA:**  $r_p \cong \underline{0.8768(69)\text{fm}}$  (ep atom) hydrogen spectrum  
(2008) (Main sensitivity - Lamb Shift)

Depends on Rydberg Constant

$R_\infty = 1.0973731568527(73) \times 10^7 \text{m}^{-1}$

**known to 13 significant figures!**

$R_\infty \cong \alpha^2 m_e c / 2h$  "One of the Two most accurately measured fundamental physical constants" **What is better known?**

## 3.ii) Muon Anomalous Magnetic Moment

1957 Garwin, Lederman & Weinrich study  $\pi \rightarrow \mu \nu$ ,  $\mu \rightarrow e \nu \nu$   
found parity violation & measured  $g_\mu = 2.00 \pm 0.10$

Parity Violation Decay  $\rightarrow$  Self Analyzing Polarimeter  
led to Three Classic CERN Exps. ending in 1977

“The Last  $g_\mu - 2$  Experiment”

- Until Experimental E821 at BNL (2004 Final)
- $a_\mu^{\text{exp}} \equiv (g_\mu - 2)/2 = 116592089(54)_{\text{stat}}(33)_{\text{sys}} \times 10^{-11}$

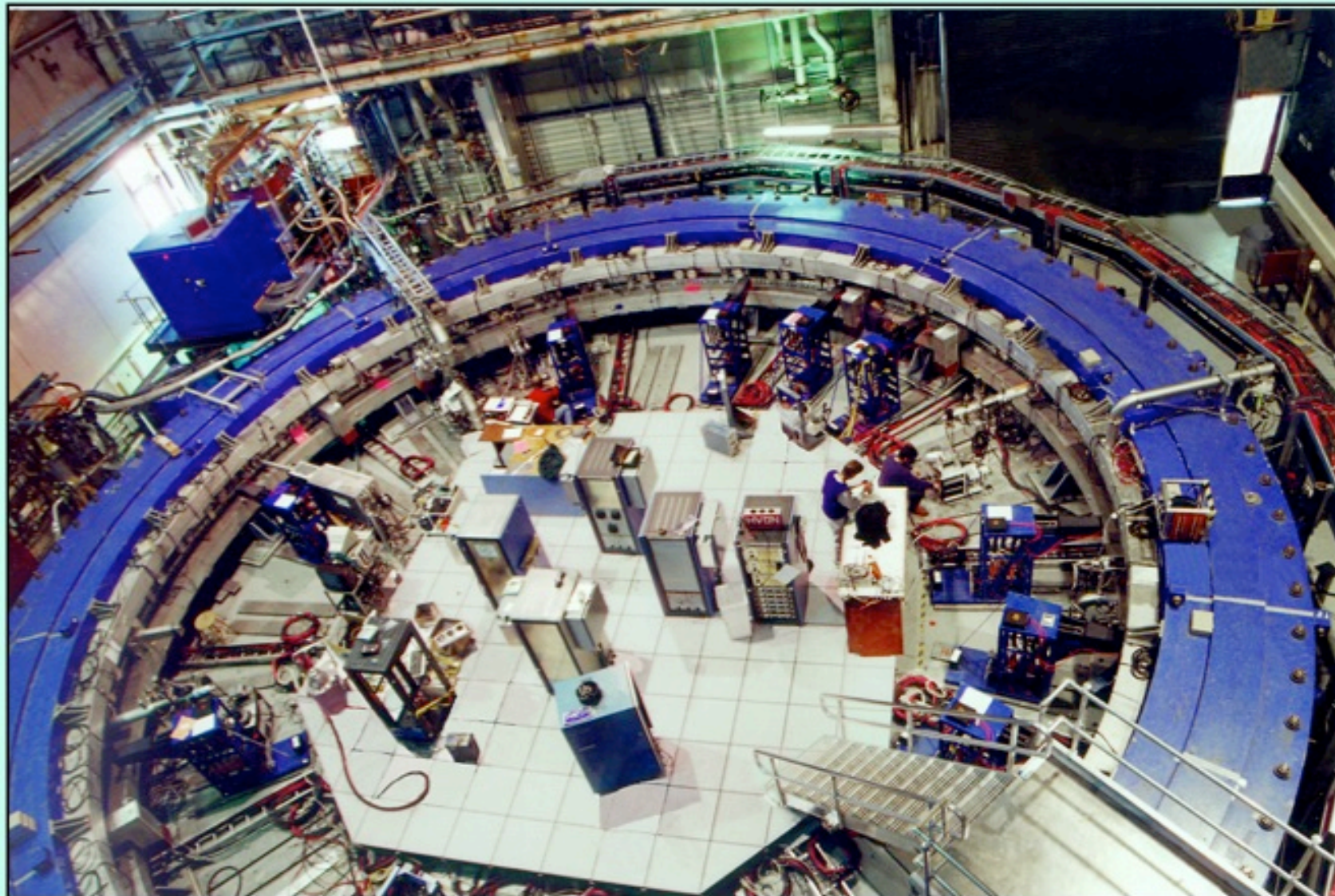
$$= \underline{116592089(63)} \times 10^{-11}$$

Factor of 14 improvement over CERN results

(Proposed Future Factor 4 Improvement at FNAL)

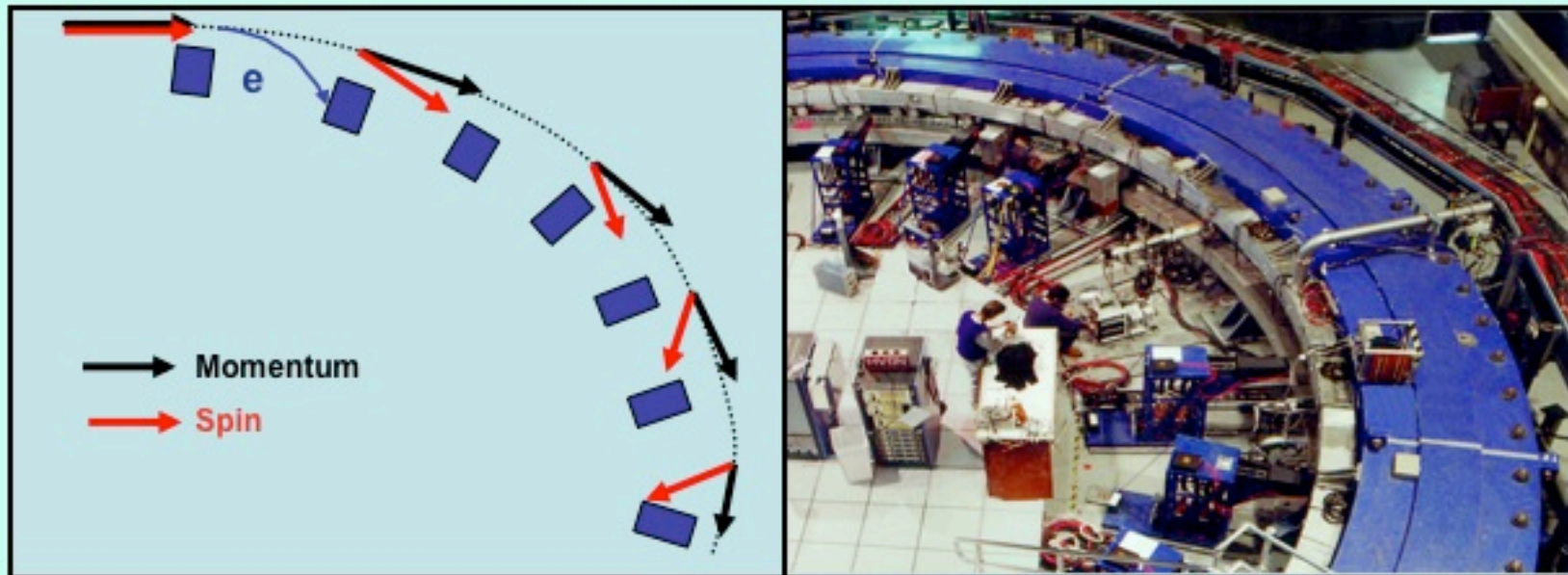
**D. Hertzog, B.L. Roberts...**

# BNL Muon $g-2$ Experiment



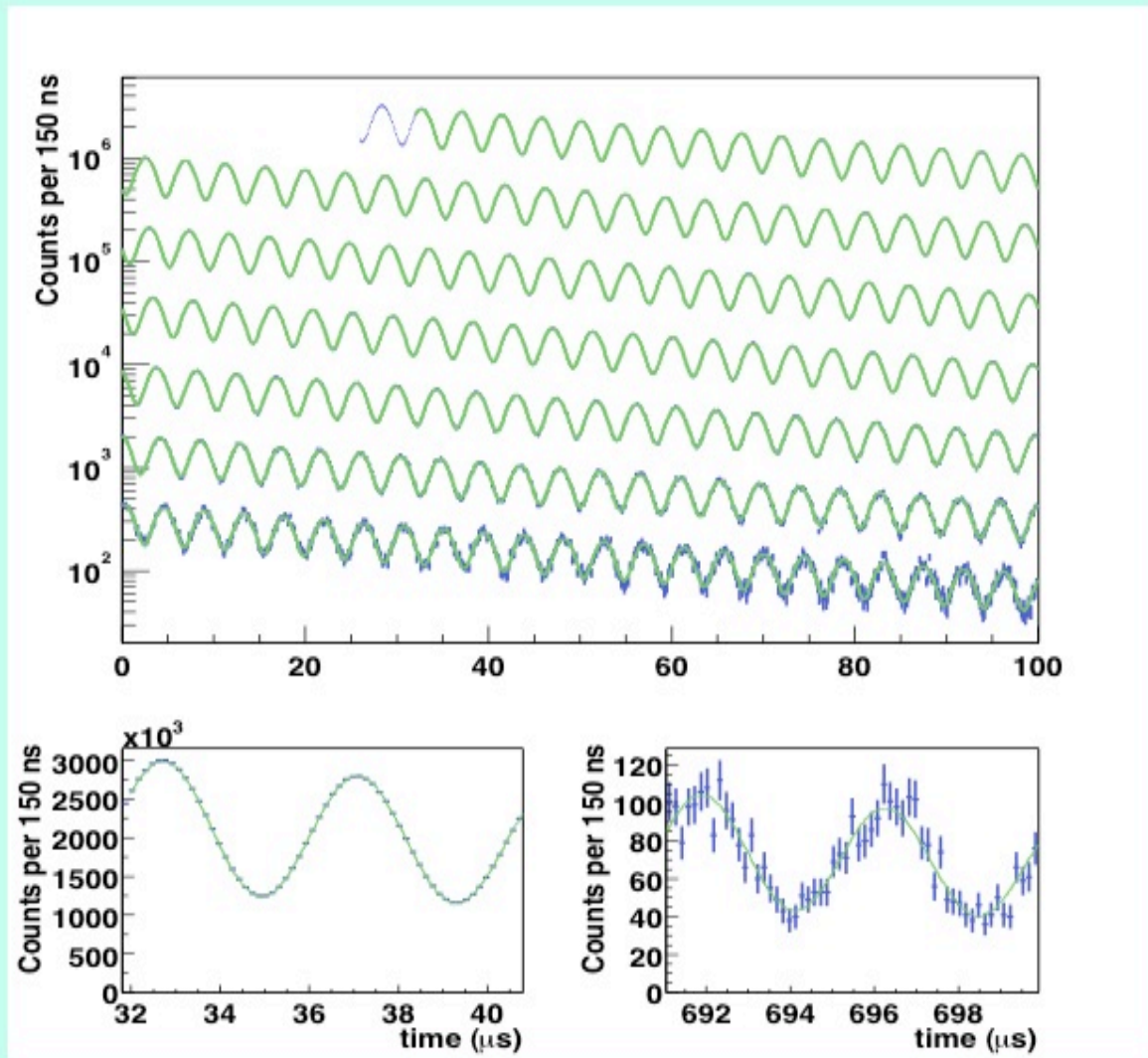


- $a_{\mu}$  is proportional to the difference between the spin precession and the rotation rate



$$\Delta\omega = \omega_a = \left( \frac{g - 2}{2} \right) \frac{eB}{mc}$$

$$N(t) = N_0 e^{-t/\tau} [1 + A \cos(\omega_a t + \phi)]$$



# Standard Model Prediction

$$a_{\mu}^{\text{SM}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Hadronic}}$$

## QED Contributions:

- $a_{\mu}^{\text{QED}} = 0.5(\alpha/\pi) + 0.765857425(17)(\alpha/\pi)^2 +$   
 $24.05050996(32)(\alpha/\pi)^3 +$   
 $\underline{130.8796(63)}(\alpha/\pi)^4 +$   
 $753.29(1.04)(\alpha/\pi)^5 + \dots$

## 2012 Update: Aoyama, Hayakawa, Kinoshita, & Nio

$$\alpha^{-1}(^{87}\text{Rb}) = 137.035999049(90)$$

$$a_{\mu}^{\text{QED}} = \underline{116584718.864(36)} \times 10^{-11} \text{ Very Precise!}$$

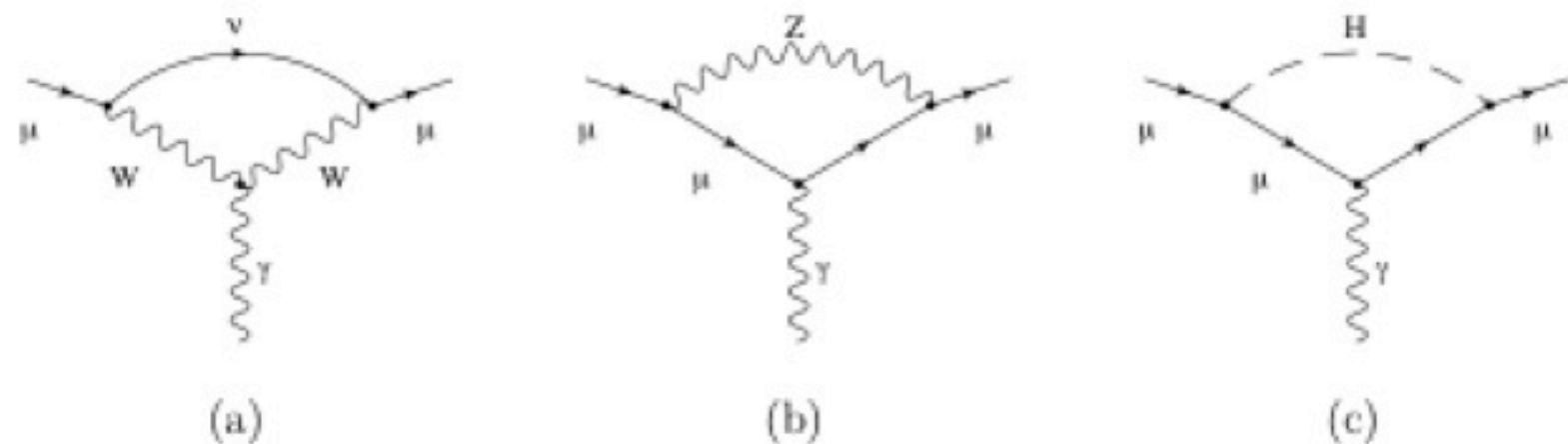


Figure 2: One-loop electroweak radiative corrections to  $a_\mu$ .

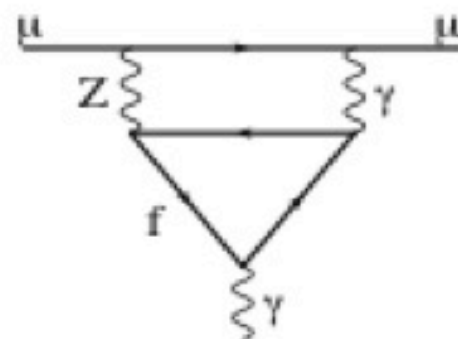


FIG. 3: Effective  $Z\gamma\gamma^*$  coupling induced by a fermion triangle, contributing to  $a_\mu^{\text{EW}}$ .



## Electroweak Loop Effects

$a_{\mu}^{EW}(1 \text{ loop}) = \underline{194.8 \times 10^{-11}}$  original goal of E821

$a_{\mu}^{EW}(2 \text{ loop}) = \underline{-40.3(1.0) \times 10^{-11}}$  (Higgs Mass = 126 GeV)

3 loop EW leading logs very small  $O(10^{-12})$

•  $a_{\mu}^{EW} = \underline{154(1) \times 10^{-11}}$  ***Non Controversial***

## • Hadronic Contributions (HVP & HLBL)

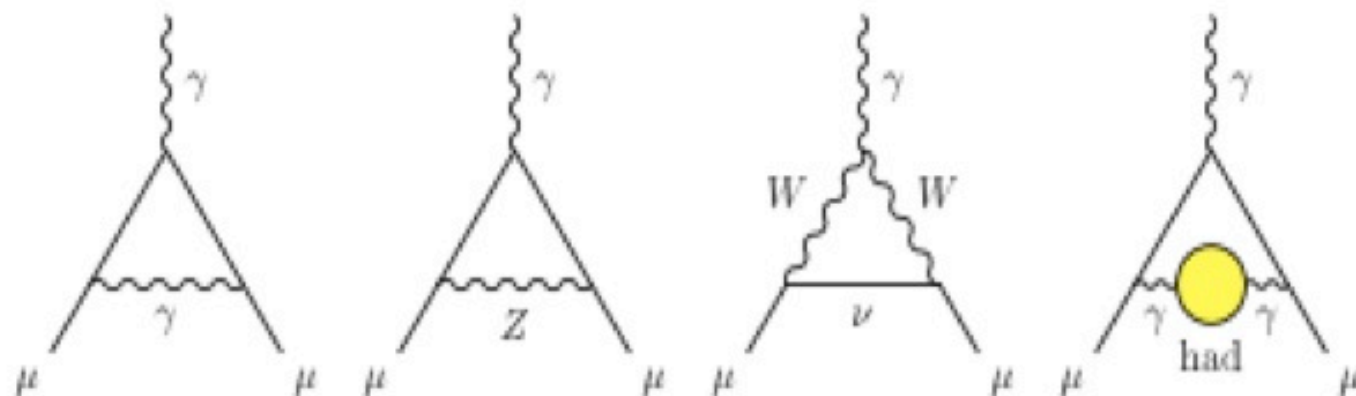
$a_{\mu}^{\text{Had}}(\text{V.P.})^{\text{LO}} = \underline{6923(40)(7) \times 10^{-11}}$  (Hoecker update 2010)

$a_{\mu}^{\text{Had}}(\text{V.P.})^{\text{NLO}} = -98(1) \times 10^{-11}$

$a_{\mu}^{\text{Had}}(\text{LBL}) = 105(26) \times 10^{-11}$  (Consensus?)

$a_{\mu}^{\text{SM}} = \underline{116591803(49) \times 10^{-11}}$  (*Future Improvement?*)

$\Delta a_{\mu} = a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = \underline{276(63)(49) \times 10^{-11}}$  (***3.5 $\sigma$  deviation!***)



**Figure 1:** Representative diagrams contributing to  $a_{\mu}^{\text{SM}}$ . From left to right: first order QED (Schwinger term), lowest-order weak, lowest-order hadronic.

From  $e^+e^- \rightarrow \text{hadrons}$  data + dispersion relation

$$a_{\mu}^{\text{Had}}(\text{V.P.})^{\text{LO}} = \underline{6923(40)(7)} \times 10^{-11} \text{ (Hoecker update 2010)}$$

$$\underline{3 \text{ loop}} = a_{\mu}^{\text{Had}}(\text{V.P.})^{\text{NLO}} + a_{\mu}^{\text{Had}}(\text{LBL})$$

$$a_{\mu}^{\text{Had}}(\text{V.P.})^{\text{NLO}} = -98(1) \times 10^{-11}$$

$$a_{\mu}^{\text{Had}}(\text{LBL}) = 105(26) \times 10^{-11} \text{ (Consensus?)}$$

Prades, de Rafael, Vainshtein

$$a_{\mu}^{\text{Had}} = 6930(40)(7)(26) \times 10^{-11} \approx 46 a_{\mu}^{\text{EW}}$$

$$a_{\mu}^{\text{SM}} = \underline{116591803(49)} \times 10^{-11}$$

## Comparison of Experiment and Theory (Most Recent)

- $\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 276(63)(49) \times 10^{-11}$  ( $3.5\sigma!$ )

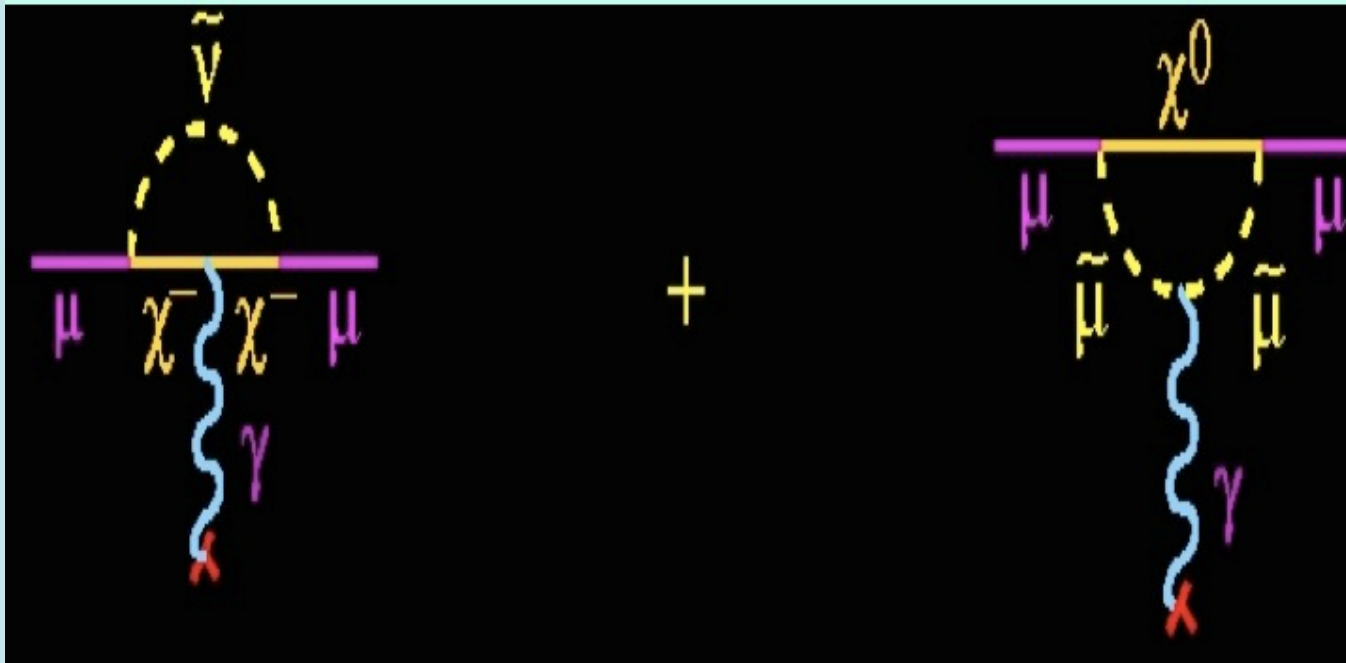
**This is a very large deviation!**

Remember, the EW contribution is  
only  $154 \times 10^{-11}$

**New Physics Nearly 2x Electroweak?**

Why don't we see it in other measurements?

3.2 “New Physics” Effects  
\_SUSY 1 loop  $a_\mu$  Corrections  
**(Most Likely Scenario)**



- SUSY Loops are like EW, but depend on:
- 2 spin 1/2  $\chi^-$  (charginos)
- 4 spin 1/2  $\chi^0$  (neutralinos) including dark matter!
- spin 0 sneutrinos and sleptons with mixing
  
- Enhancement  $\tan\beta = \langle\phi_2\rangle / \langle\phi_1\rangle \sim 3-40!$

## Interpretations

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 276(80) \times 10^{-11} \quad (3.5\sigma!)$$

### Generic 1 loop SUSY Contribution:

$$a_\mu^{\text{SUSY}} = (\text{sgn}\mu) 130 \times 10^{-11} (100 \text{ GeV} / m_{\text{susy}})^2 \tan\beta$$

$$\tan\beta \approx 3-40, \quad m_{\text{susy}} \approx 100-500 \text{ GeV} \quad \text{Some LHC Tension}$$

Other Explanations: *Hadronic e<sup>+</sup>e<sup>-</sup> Data? HLBL(3loop)?*

**Multi-Higgs Models**

**Extra Dimensions < 2 TeV**

\* Dark Photons  $\sim 10-200 \text{ MeV}$ ,  $\alpha' = 10^{-8}$

**Light Higgs Like Scalar < 10 MeV?**

## Low Mass New Physics & g-2

Dark Photon of g-2 interpretation easy to find at JLAB or Mainz (Bremsstrahlung)  $e+X \rightarrow e+X+\gamma_d$  ( $\gamma_d \rightarrow e^+e^-$ )

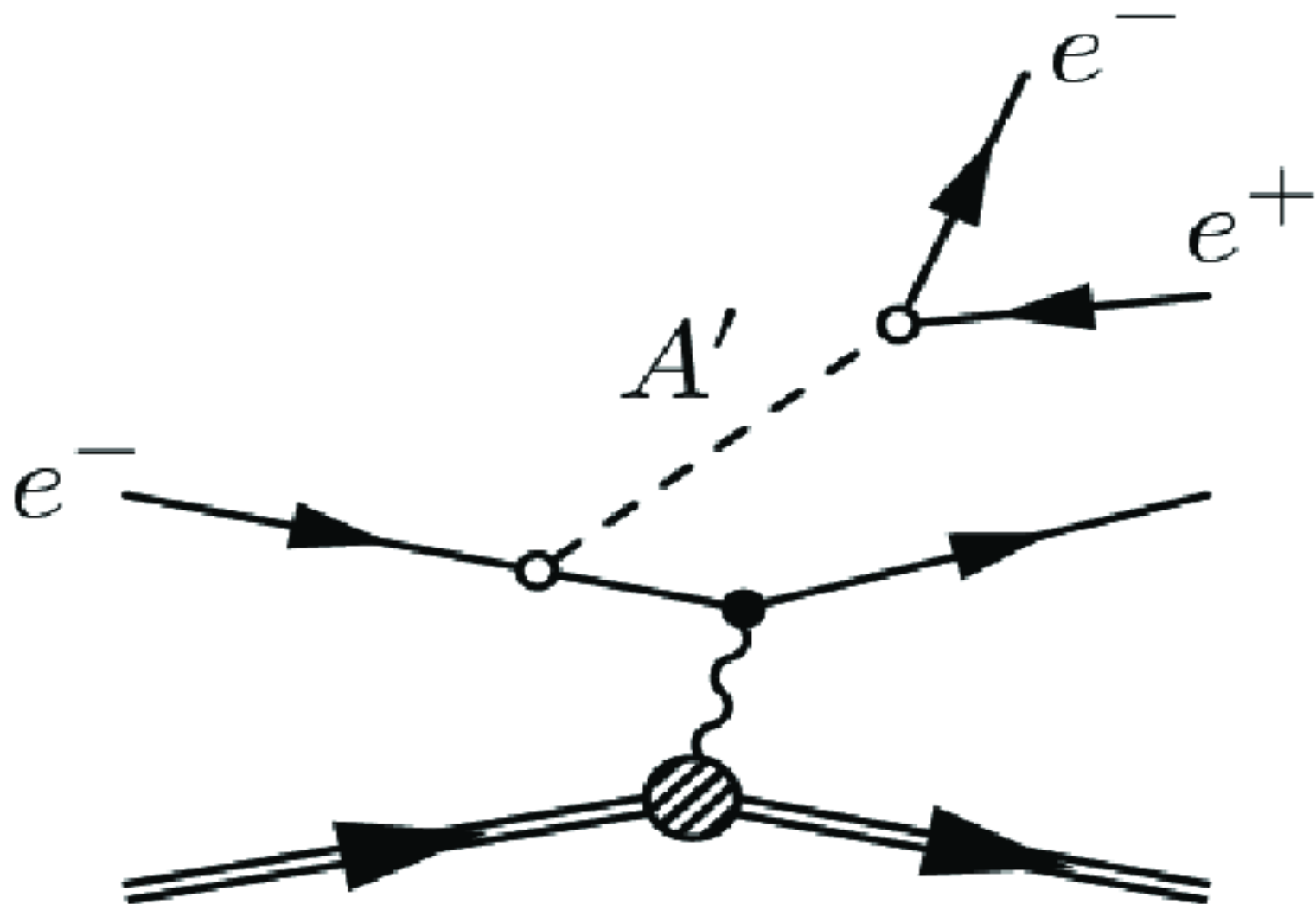
*Would Revolutionize Physics*

*Contact with Dark Matter!*

*Very Light Higgs  $\leq 10\text{MeV}$  could also account for discrepancy*

***Who Ordered That?***





#### 4.) ***Muonic Hydrogen Lamb Shift***

In an effort to precisely determine  $r_p$

**New PSI  $\mu p$  atomic Lamb shift experiment**

$$\Delta E(2P_{3/2}-2S_{1/2})=209.9779(49)-5.2262r_p^2+0.0347r_p^3 \text{ meV}$$

***R. Pohl, A. Antognini et al. Nature July 2010***

***Very Elegant!***

**Stop  $\mu^-$  in Hydrogen, About 1% populate 2S (1 $\mu$ sec)**

**Excite resonance with laser to 2P $\rightarrow$ 1S**

$\mu p$  atomic Lamb Shift **very** sensitive to  $r_p$

$$(m_\mu/m_e)^3 = 8 \times 10^6 \text{ enhancement}$$

Proton Finite Size  $\approx -2\%$

***20ppm experiment***

***12years in the making (1998-2010)***

$$\Delta E(2P_{3/2}-2S_{1/2})^{\text{exp}} = 206.2949 \pm 0.0032 \text{ meV}$$

$$r_p = \underline{0.84184(67)\text{fm}} \quad (\mu\text{p atom})$$

*10x More Precise & 5 sigma below ep value!*

$$r_p \cong \underline{0.8768(69)\text{fm}} \quad (\text{ep atom})$$

Confirmation from ep scattering

$$r_p \cong \underline{0.879(8)\text{fm}} \quad (\text{Recent Mainz})$$

$$r_p \cong \underline{0.875(10)\text{fm}} \quad (\text{Recent JLAB})$$

***Current Electron Average:  $r_p = \underline{0.8772(46)\text{fm}}$***

***8 sigma below  $\mu\text{p atom}$ !***

Atomic ep Theory? Rydberg Constant( $R_\infty$ ) (Off by  $5\sigma$ ?)

**$R_\infty$  known to 13 significant figures!**

$$=1.0973731568527(73)\times 10^7\text{m}^{-1}$$

”One of the Two most accurately measured fundamental physical constants”.

***Could  $R_\infty$  really be wrong?***

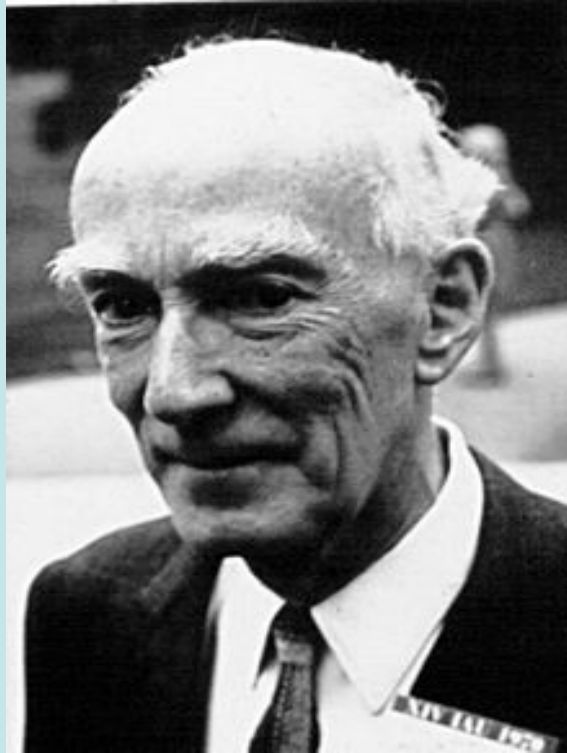
***also***

***What about ep scattering? Wrong!***

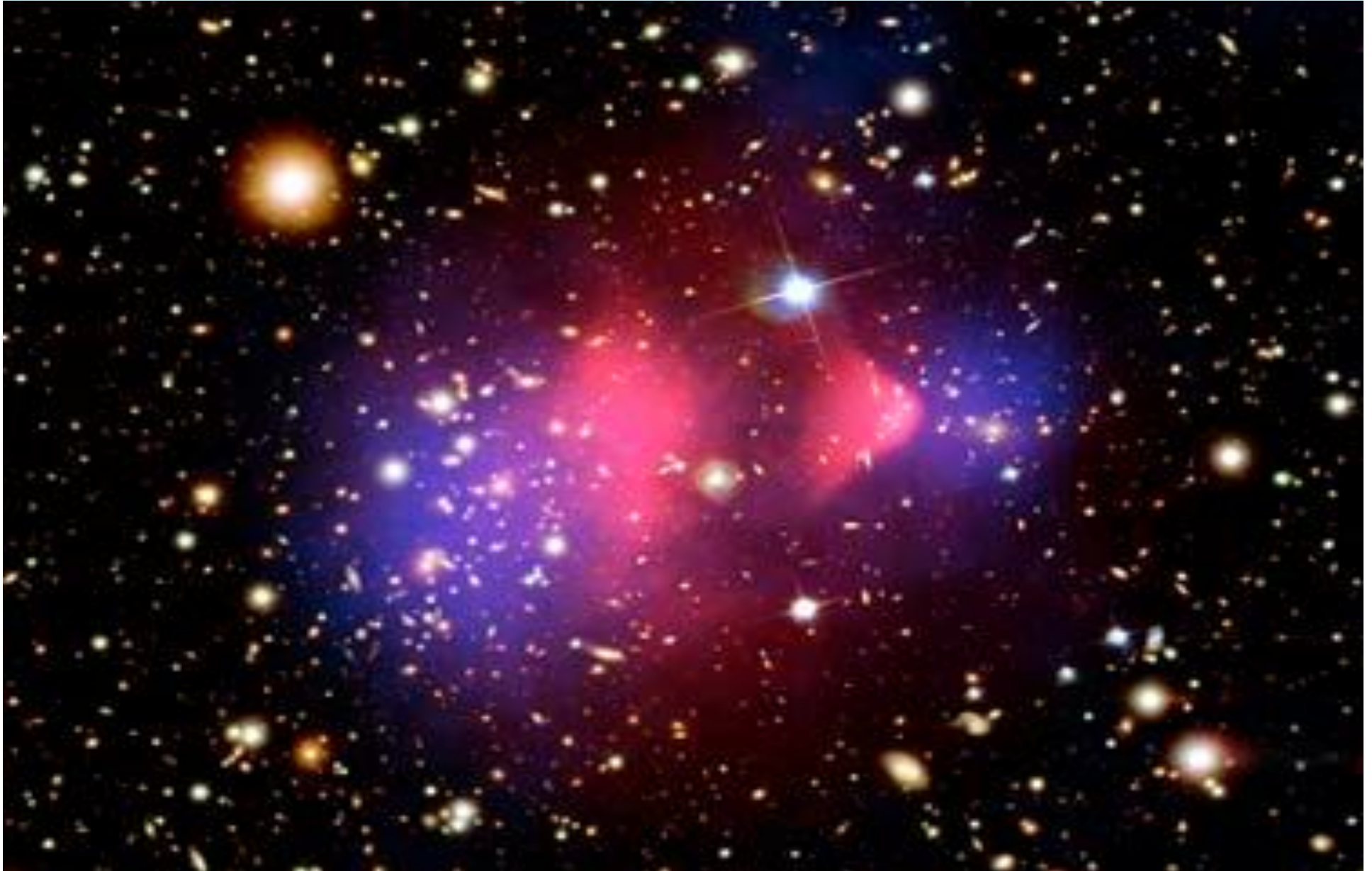
**Perhaps the most likely solution**

*(About the same time antiparticles were being discovered)*  
*1932-33's Astronomers start to see*  
*"Dark Matter" Evidence!*

## **Jan Ort & Fritz Zwicky**



# *Bullet Galaxy Cluster*



## ***What is the Dark Matter?***

Light Matter-Ordinary Particles (Galaxies, Stars, Us)

= 3-4% Of Universe (many varieties)

Dark Matter = 22% Of Universe – Gravitational Interactions

Dark Energy = 75% Of Universe – Cosmological Constant

***Is dark matter a single **stable** new elementary particle?***

***How Heavy is it? Spin (0,1/2,1,3/2)?***

***Does it interact only gravitationally?***

***Does it have antiparticle partner(s)? (Asymmetry?)***

Are there many species of dark particles (most unstable)

Does Dark Matter have gauge interactions? Dark Charge?

## **The Hunt For Dark Particles**

- Underground Searches for Dark Matter Particles (WIMPS)

### **Conflicting Experimental Results**

Astrophysics - Possible Hints of Dark Particle Annihilations

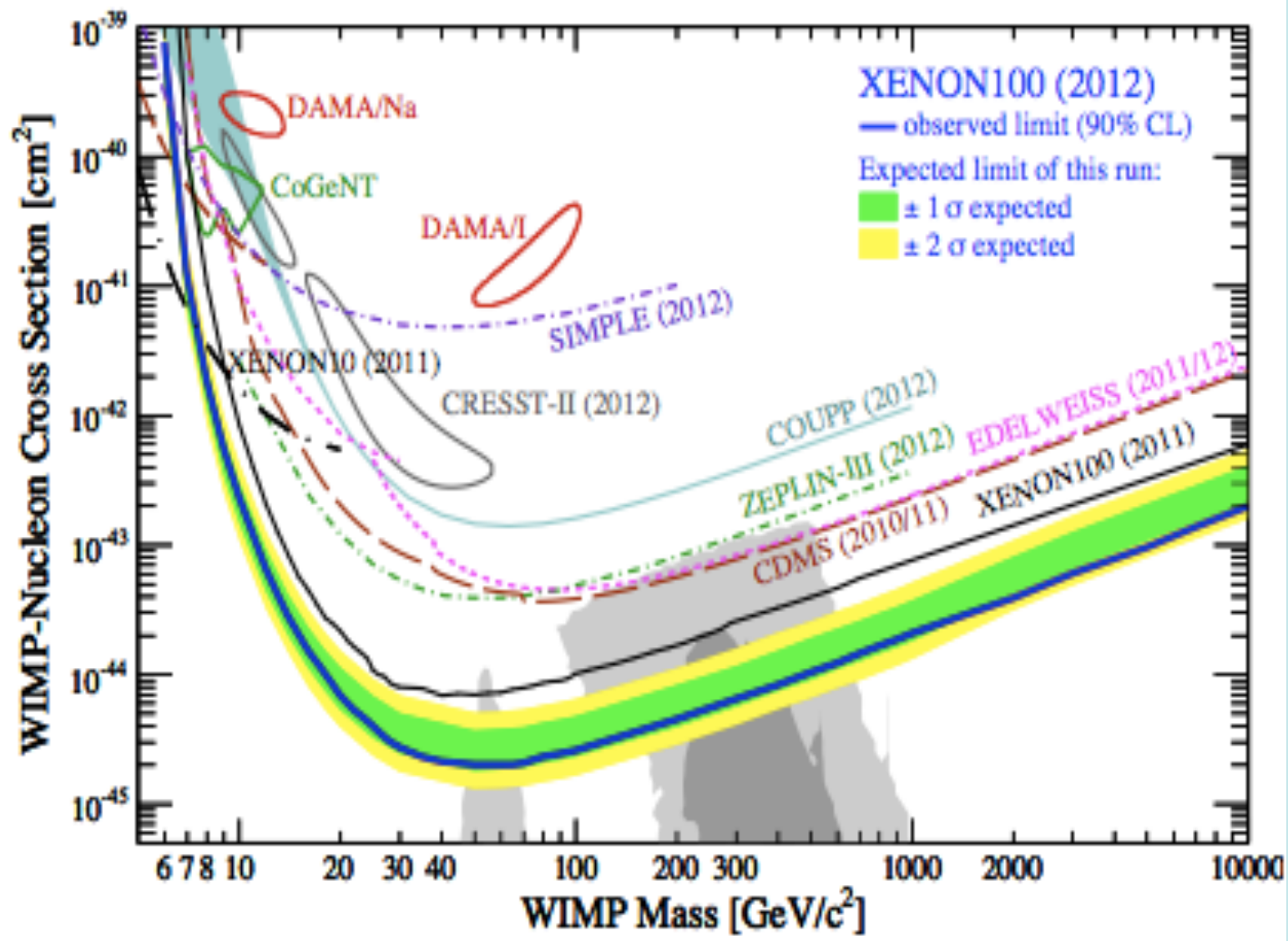
LHC (Supersymmetry – Other?) No direct detection yet

### **The Dark Photon – A Possible Portal to Dark Matter**

What if dark particles interact weakly with one another via a new massive but relatively “light”  $\gamma_d$  (Dark Photon) ?

***Can we find evidence for such a particle?***





# Astrophysics: Hints of Dark Particle Annihilations

## Light or Heavy Dark Matter Particles?

**Positron ( $e^+$ ) Excesses at high energies(?)**

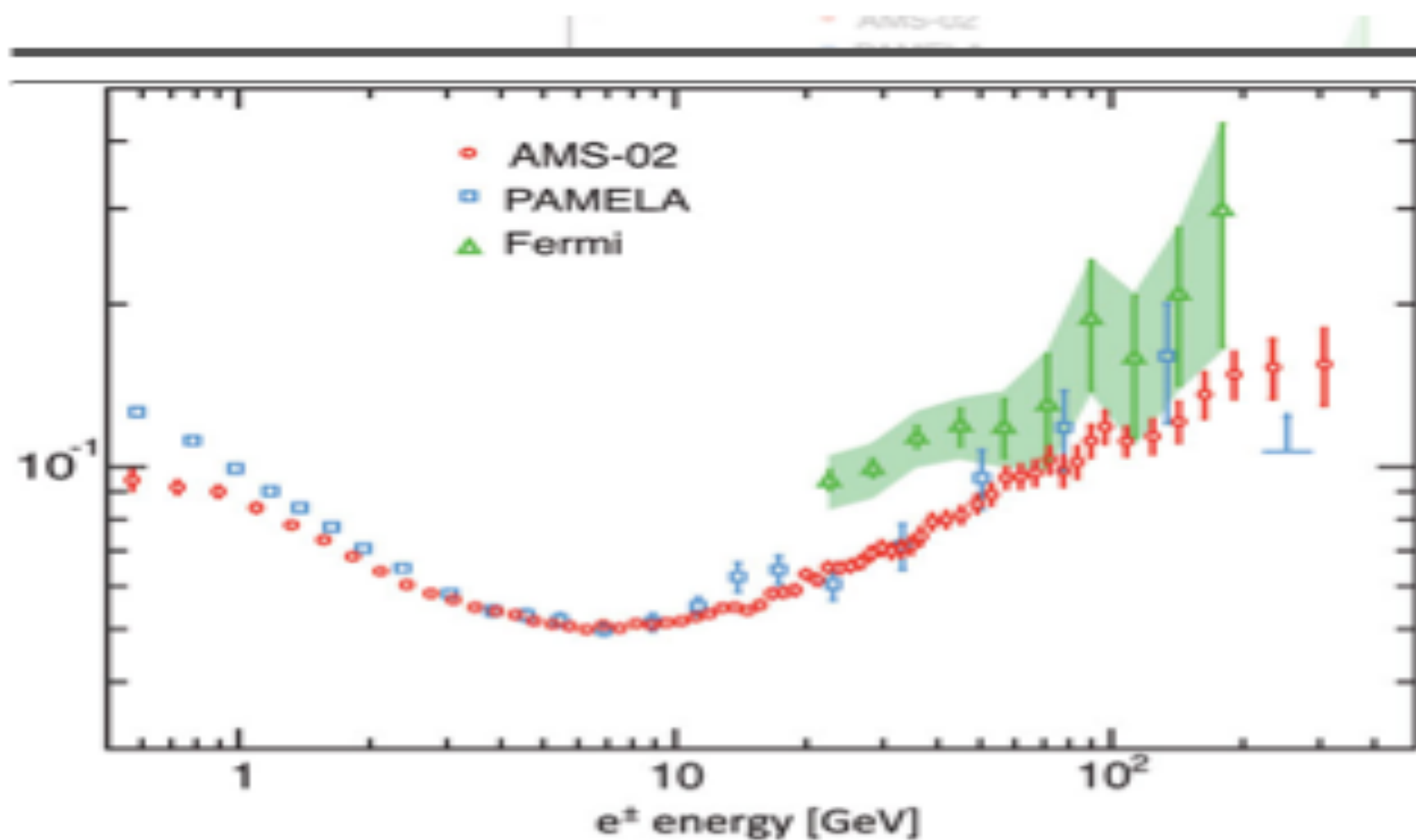
Pamela, Fermi, AMS (Heavy Dark Matter) > TeV? (Unlikely Interpretation?)

Fermi  $\gamma$ -ray Excess from Galactic Center

**Light  $\sim 10$  GeV Dark matter annihilations ( $\rightarrow e^+e^-, \mu^+\mu^-, \tau^+\tau^-$ )**

Both Interesting Effects

Interpretations?



positron fraction as measured by the AMS (red circles) from 1 to 350 GeV. (Courtesy: *Phys. Rev. Lett.* **110** 141102)

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## $\gamma_d$ coupling to our particle world

- **Very Weak < 0.0001x electromagnetism**

Nevertheless, produce in electron scattering

detect  $\gamma_d \rightarrow e^+e^-$

Experiments at JLAB and MAMI (Mainz)

More planned for the future

So far, no direct signal

## Outlook

i) Exciting New Lepton Anomalous Magnetic Moments Ahead

Low energy potential for: SUSY, Multi-Higgs,.. Dark Photon

ii)  $\sin^2\theta_W$ ,  $m_W$  &  $m_t$  improvements expected

iii) PERHAPS the LHC will directly uncover “New Physics”!

***Precision Experiments are Hard***

**Challenges Advance Physics**

***Remember Michelson the Master of Light***