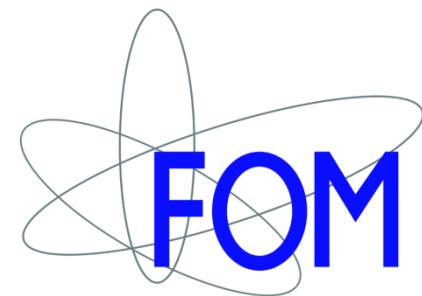


# Limits on Lorentz Violation in weak decays



*Keri Vos*

*J.P. Noordmans, H.W. Wilschut and R.G.E. Timmermans  
A.Sytema & C.J.G. Onderwater*

*University of Groningen*

*KKV, et al, PLB 729,112 (2014)*



# Outline



✗ Testing Lorentz Violation

✗ Efforts in weak decays

✗ Results for non-leptonic Kaon decay

- ✗ Kloe data

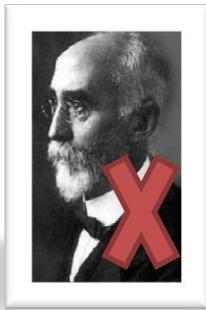
- ✗ Theory

- ✗ Theoretical Model

✗ Conclusion and Outlook



## Quantum Gravity



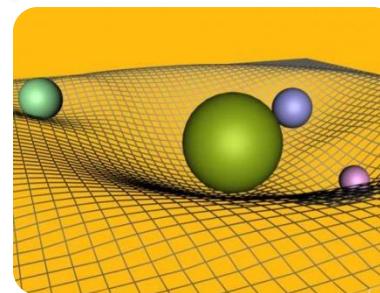
**CRT**

O.W. Greenberg, PRL 89, 231602 (2002)

Vacuum expectation values  
for tensor fields

Planck scale  
 $10^{19}$  GeV

Elementary Particles in the Standard Model		
FERMIONS		
u UP	c CHARM	t TOP
d DOWN	s STRANGE	b BOTTOM
LEPTONS		
v <sub>e</sub> ELECTRON NEUTRINO	v <sub>μ</sub> MUON NEUTRINO	v <sub>τ</sub> TAU NEUTRINO
e ELECTRON	μ MUON	τ TAU
BOSONS		
γ PHOTON	g GLUON	Z <sup>0</sup> WEAK FORCE
FORCE-CARRIERS		
W <sup>±</sup> WEAK FORCE		
h HIGGS		





## Quantum Gravity

Gauge structure  
(Renormalizability)  
Energy & momentum  
conservation  
Causality  
Spin-statistics

Planck scale

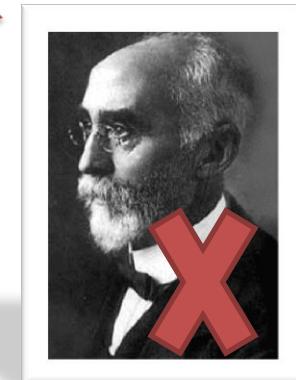
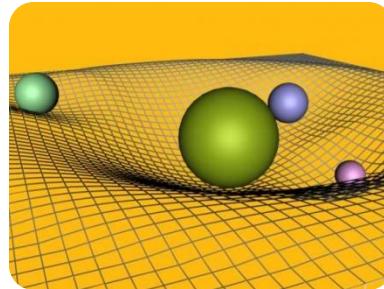
$10^{19}$  GeV

100 GeV

D. Colladay and V.A. Kostelecky, Phys. Rev. D 58, 116002 (1998)

# SME

Elementary Particles in the Standard Model		
FERMIONS		
u UP	c CHARM	t TOP
d DOWN	s STRANGE	b BOTTOM
LEPTONS		
$\nu_e$ ELECTRON NEUTRINO	$\nu_{\mu}$ MUON NEUTRINO	$\nu_{\tau}$ TAU NEUTRINO
e ELECTRON	$\mu$ MUON	$\tau$ TAU
BOSONS		
$\gamma$ PHOTON	$g$ GLUON	$Z^0$ WEAK FORCE
FORCE-CARRIERS		
$W^+$ WEAK FORCE	$h$ HIGGS	



# Testing Lorentz violation



Constrain underlying fundamental theory.

## SME

Weak sector relatively unexplored!

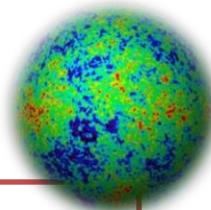


- Muon g-2
- Neutrino oscillations
- Matter interferometry
- Oscillations of K, B, D mesons
- QED tests in Penning traps

- Particle-antiparticle comparisons
- Spectroscopy of hydrogen and antihydrogen

- Baryon asymmetry
- Laboratory tests of gravity
- Clock-comparison measurements

- High-energy astrophysical observations
- Tests with microwave cavities and lasers



- CMB polarization
- Collider experiments
- Cosmological birefringence
- Dispersion from cosmological sources
- High-energy astrophysical observations

# Testing Lorentz violation

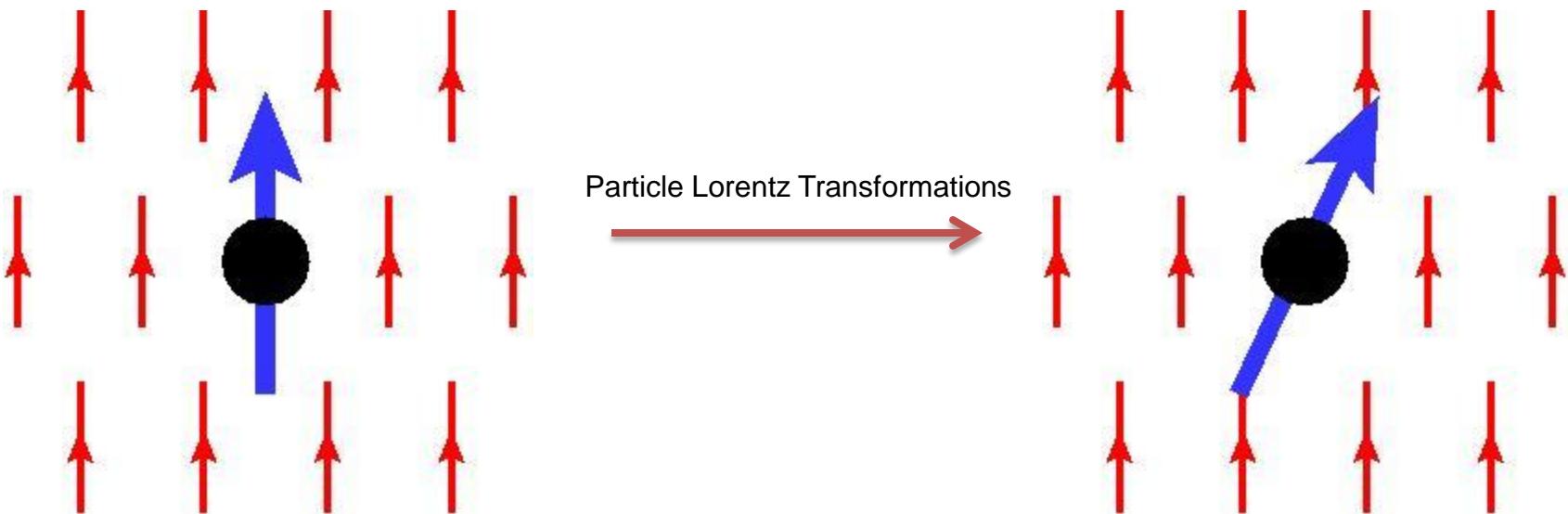


$$\mathcal{L} = -\bar{\psi}(m + a_\mu \gamma^\mu + b_\mu \gamma_5 \gamma^\mu) \psi + \frac{i}{2} \bar{\psi} (\gamma_\nu + c_{\mu\nu} \gamma^\mu + d_{\mu\nu} \gamma_5 \gamma^\mu) \tilde{\partial}^\nu \psi$$

CPT-odd Lorentz violating

CPT-even Lorentz violating

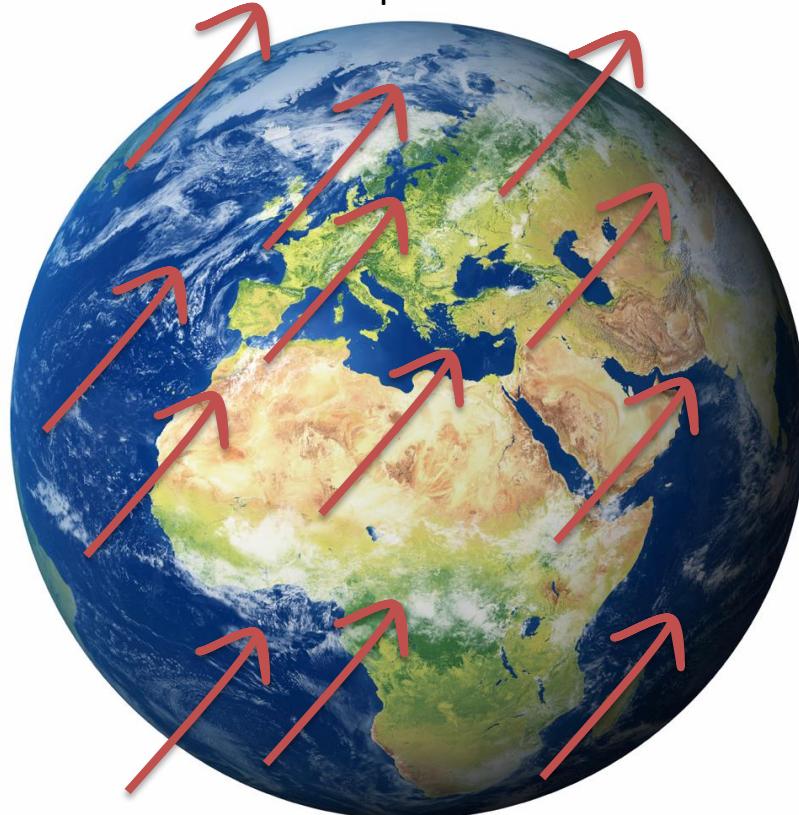
- ✓ Observer invariance maintained (coordinate independence)
- ✗ Breaking of particle Lorentz transformation (boost or rotations)



# Testing Lorentz violation



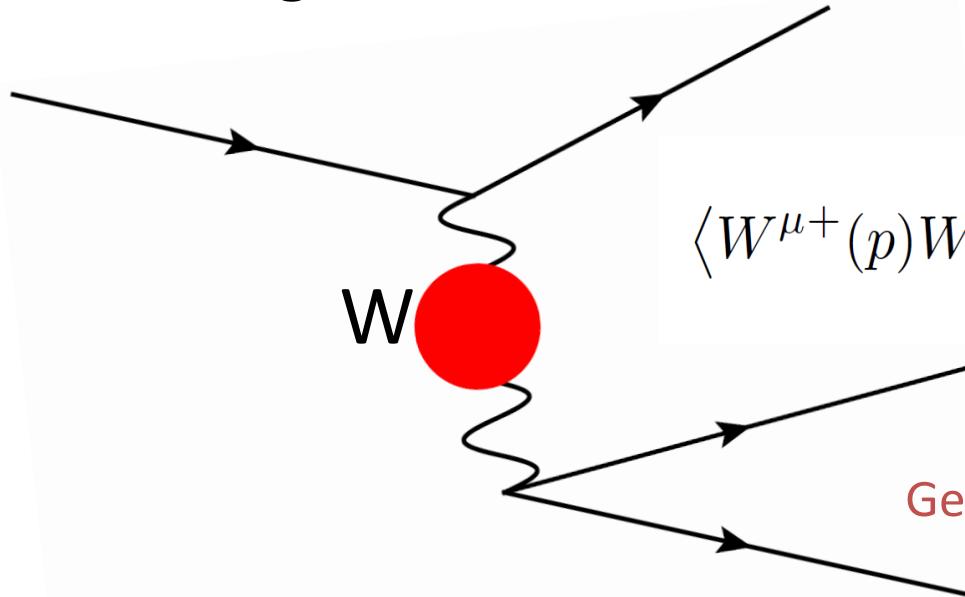
Example: preferred direction in space



- ✗ Sidereal variations
- ✗ Flip experimental setup

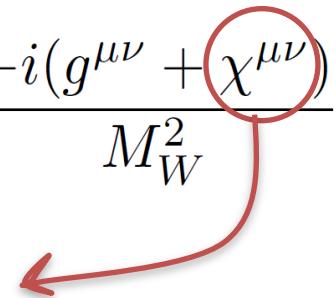


## Testing the Weak interaction



J.P. Noordmans *et al.*, Phys. Rev. C 87, 055502 (2013)

$$\langle W^{\mu+}(p)W^{\nu-}(-p) \rangle = \frac{-i(g^{\mu\nu} + \chi^{\mu\nu})}{M_W^2}$$



General Lorentz violating tensor

For example, in minimal SME,

$$\chi^{\mu\nu} = -k_{\phi\phi}^{\mu\nu} - \frac{i}{2g} k_{\phi W}^{\mu\nu} + \frac{2p_\rho p_\sigma}{M_W^2} k_W^{\rho\mu\sigma\nu}$$

No direct constraints!

# Efforts in weak decays



✗ Allowed  $\beta$  decay at KVI

S.E. Muller *et al.*, Phys. Rev. D 88, R071901 (2013)



stay tuned

✗ Forbidden  $\beta$  decay

reanalysis old experiments  
J.P. Noordmans *et al.*, PRL 111, 171601 (2013)

$$\chi < 10^{-6} - 10^{-8}$$



✗ Pion decay at MINOS

B. Altschul, Phys. Rev. D 88, 076015 (2013)



this talk

✗ Kaon decay at KLOE

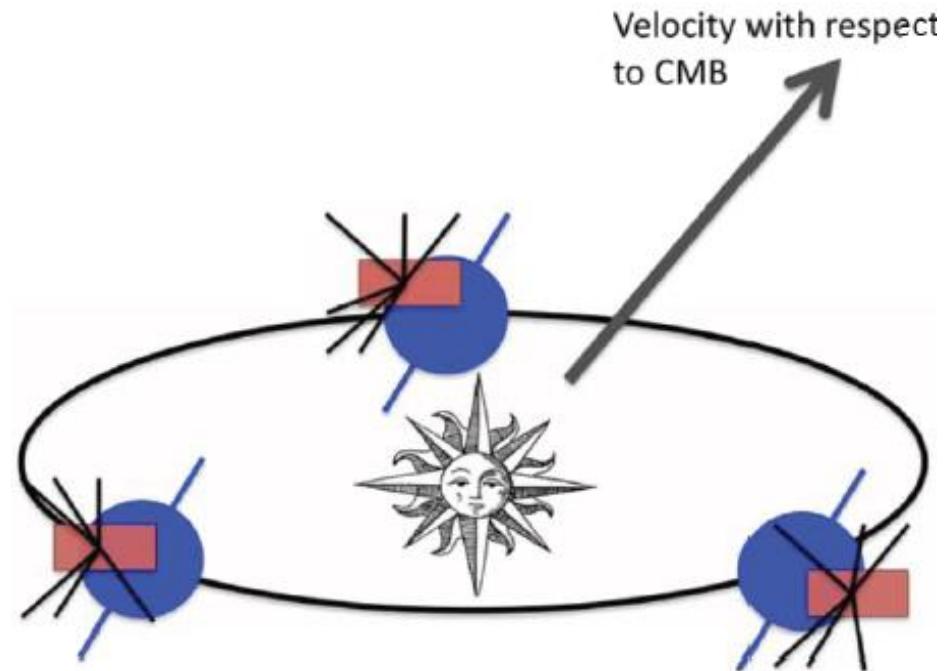
K.K. Vos *et al.*, PLB 729, 112 (2014)



# Directional dependent lifetime asymmetry of neutral Kaons $K_S^0 \rightarrow \pi^+ \pi^-$

$$\mathcal{A} = \frac{\tau^+ - \tau^-}{\tau^+ + \tau^-}$$

parallel      anti-parallel  
lifetime



Frame dependent: CMB-dipole frame

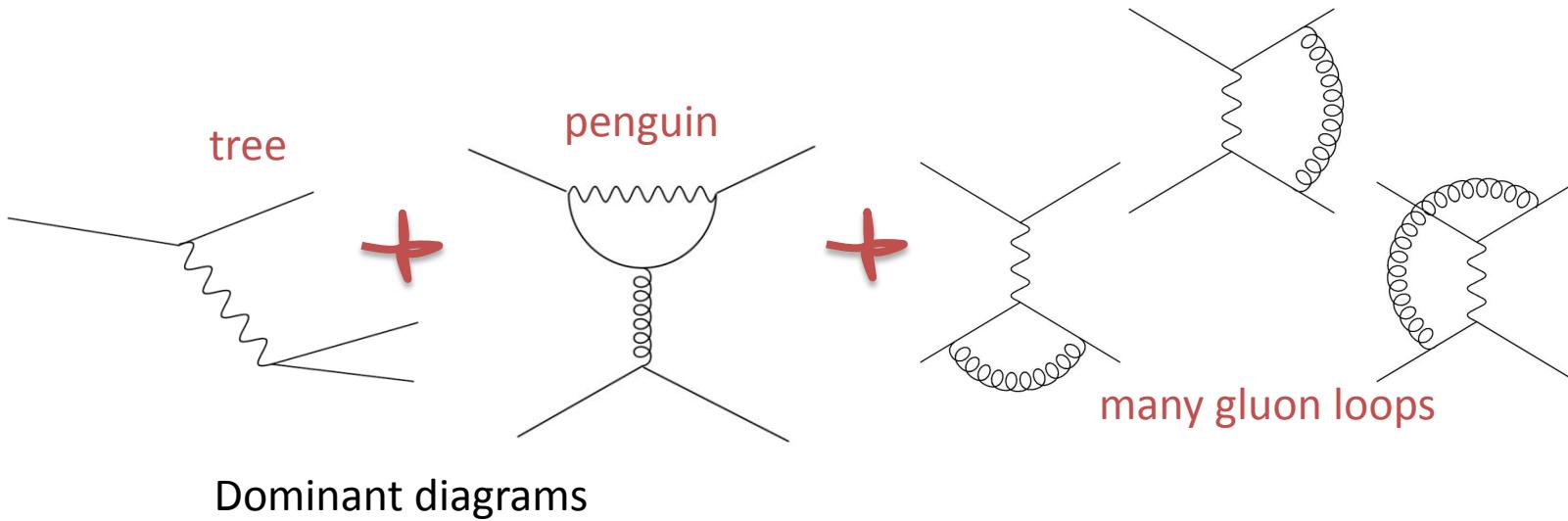
$\{\ell, b\}$	$\mathcal{A} \times 10^3$
CMB0 = {264°, 48°}	-0.2 ± 1.0 [1]
CMB0 = {264°, 48°}	-0.13 ± 0.4 [2]
CMB1 = {174°, 0°}	0.2 ± 1.0 [1]
CMB2 = {264°, -42°}	0.0 ± 0.9 [1]

[1] F. Ambrosino, Eur. Phys. J. C71, 1604(2011).

[2] A. De Angelis, Nuovo Cim. C034N3, 323 (2011).

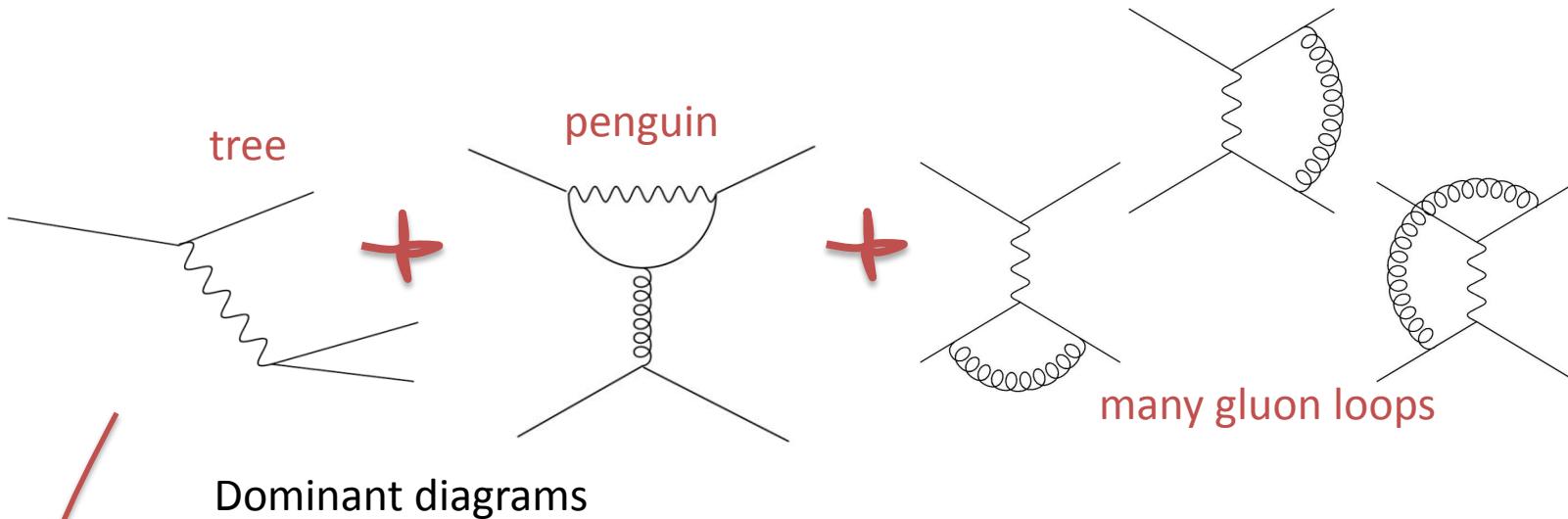


## Non-leptonic decays

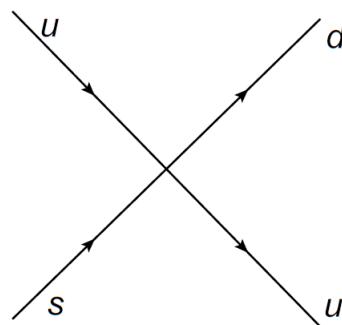




## Non-leptonic decays



In the SM



M. Shifman et al, Nucl. Phys. B120, 316(1977)

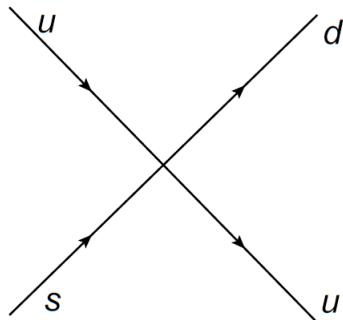
Effective Hamiltonian  $\Delta S=1$  non-leptonic

$$\mathcal{H} \sim \frac{4G_F}{2\sqrt{2}} \cos \theta_C \sin \theta_C \sum_{i=1}^6 c_i \mathcal{O}_i,$$

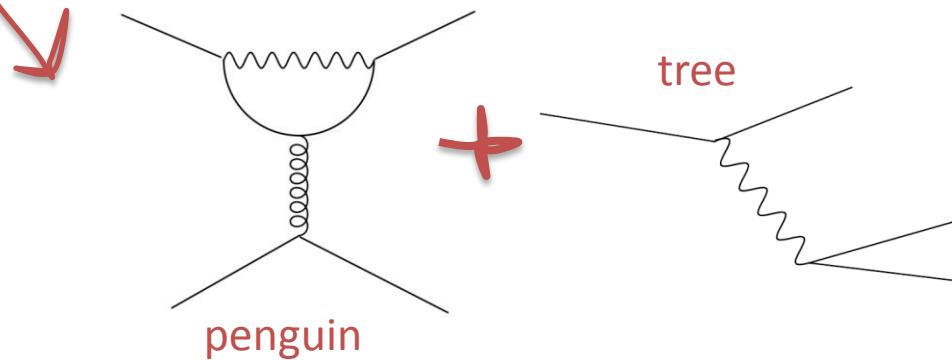


# Non-leptonic decays

In the SM



Dominant diagrams



M. Shifman et al, Nucl. Phys. B120, 316(1977)

Effective Hamiltonian  $\Delta S=1$  non-leptonic

$$\mathcal{H} \sim \frac{4G_F}{2\sqrt{2}} \cos \theta_C \sin \theta_C \sum_{i=1}^6 c_i \mathcal{O}_i,$$

$\Delta I = \frac{1}{2}$  rule ?

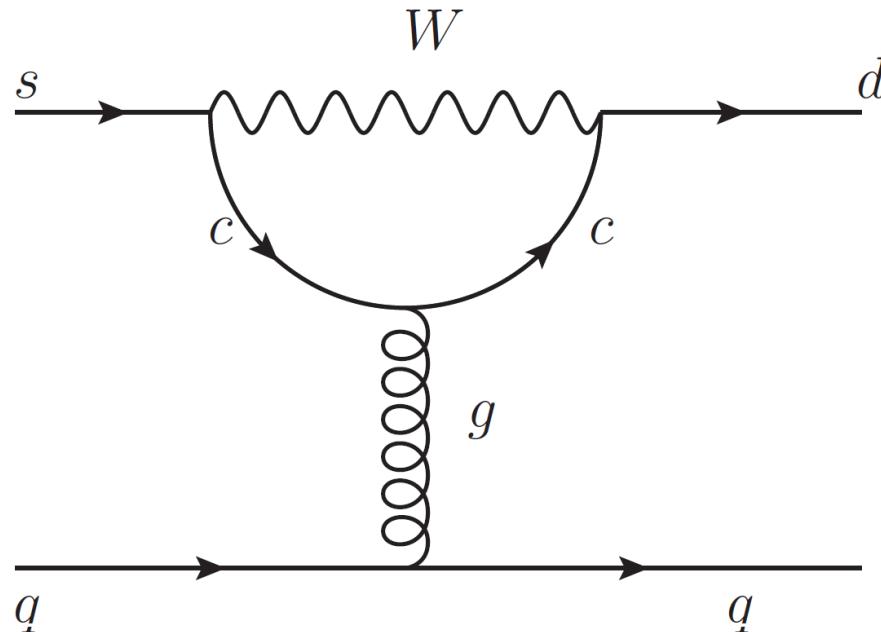


Lattice QCD

P.A. Boyle et al., PRL 110, 152001(2013)



## Penguin diagram



Enhancement due to coupling to right-handed quarks

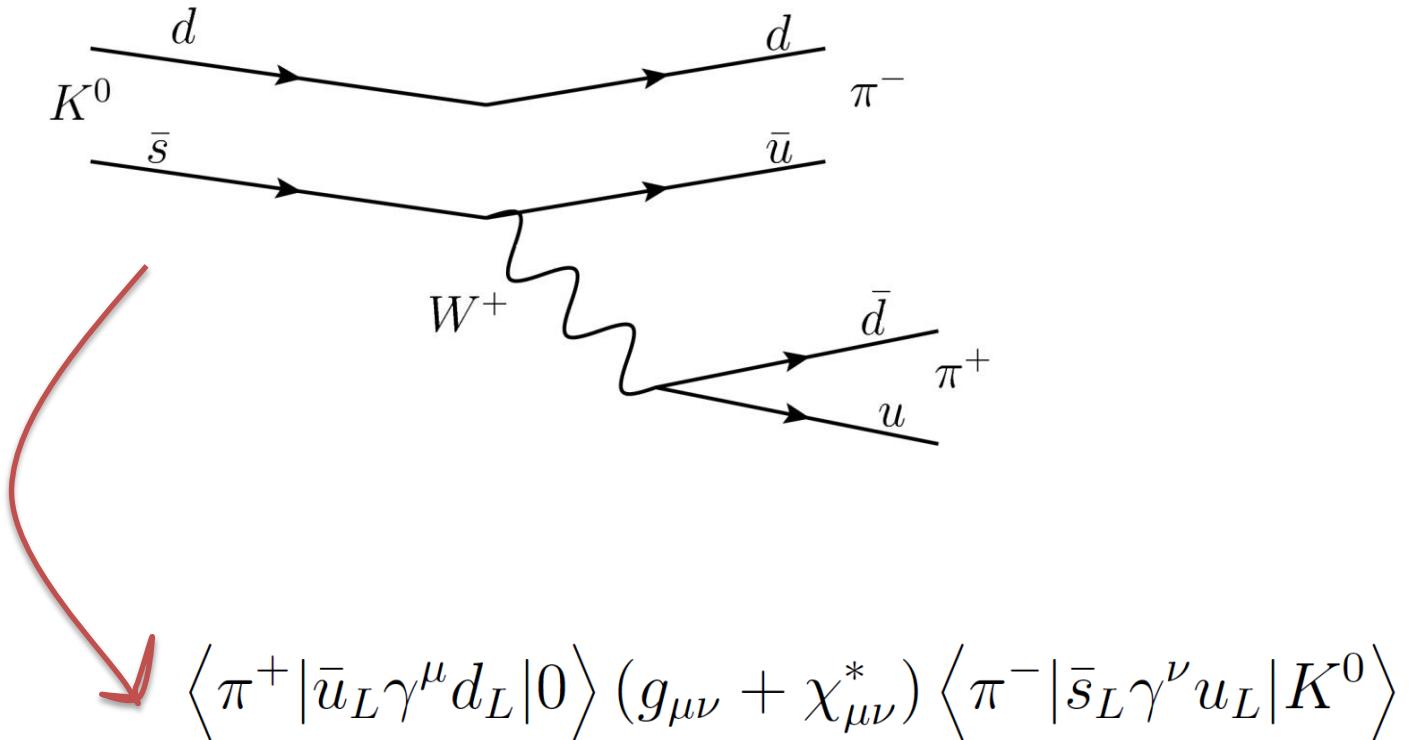
Cancels in the asymmetry  
Assume: tree-level dominant



## Tree-level diagram



Explore possibilities of non-leptonic decays



# Results: Theoretical model



CMB0 = { $264^\circ, 48^\circ$ }  
 CMB1 = { $174^\circ, 0^\circ$ }  
 CMB2 = { $264^\circ, -42^\circ$ }

$$\mathcal{A}_{\vec{n}} = - \frac{\frac{4}{3} + \frac{2}{3} \frac{m_\pi^2}{m_K^2}}{(1 - \beta_K^2) \left(1 - \frac{m_\pi^2}{m_K^2}\right)} (\chi_{i0}^r + \chi_{0i}^r) \beta_K^i = -0.343 (\chi_{i0}^r + \chi_{0i}^r) \hat{\beta}_K^i$$

↗ Real & symmetric part  
↘  $\gamma^2$  enhancement

Constraints:

$$|\chi_{\text{CMB0},0}^r + \chi_{0,\text{CMB0}}^r| < 2.9 \times 10^{-3} \text{ (95% C.L.)}$$

$$|\chi_{\text{CMB1},0}^r + \chi_{0,\text{CMB1}}^r| < 6.8 \times 10^{-3} \text{ (95% C.L.)}$$

$$|\chi_{\text{CMB2},0}^r + \chi_{0,\text{CMB2}}^r| < 5.5 \times 10^{-3} \text{ (95% C.L.)}$$

# Conclusion & Outlook



- First bounds on Lorentz violation in weak sector.
- Exploratory study in non-leptonic decays.
- Asymmetries get  $\gamma^2$  enhancement.
  - Semi-leptonic decays theoretical cleaner.
  - Other weak decays to test Lorentz Violation

potential for LHCb

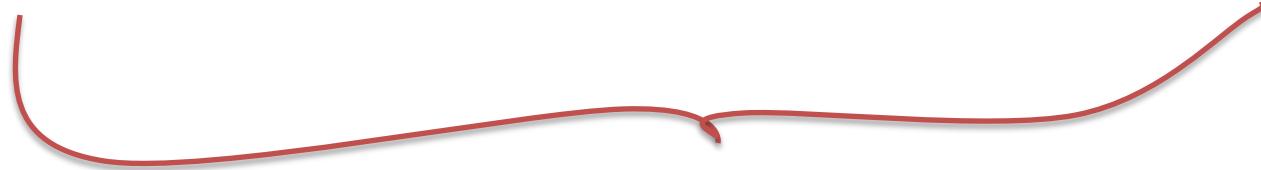
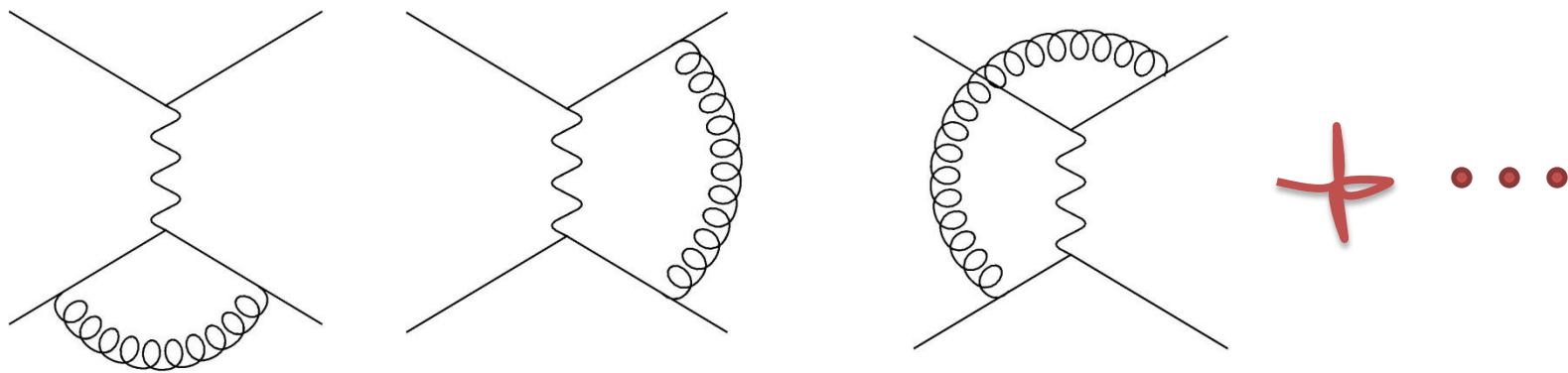
$\mu$  &  $\pi$

✓

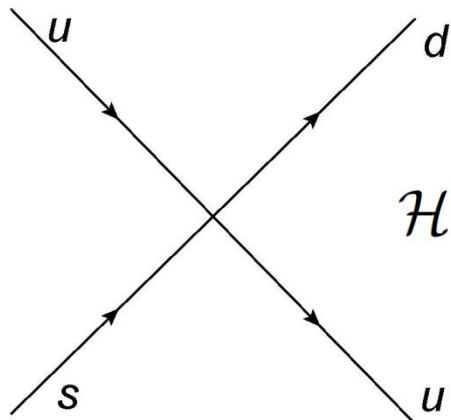
Thank you for your attention



# Results: Penguin Diagram



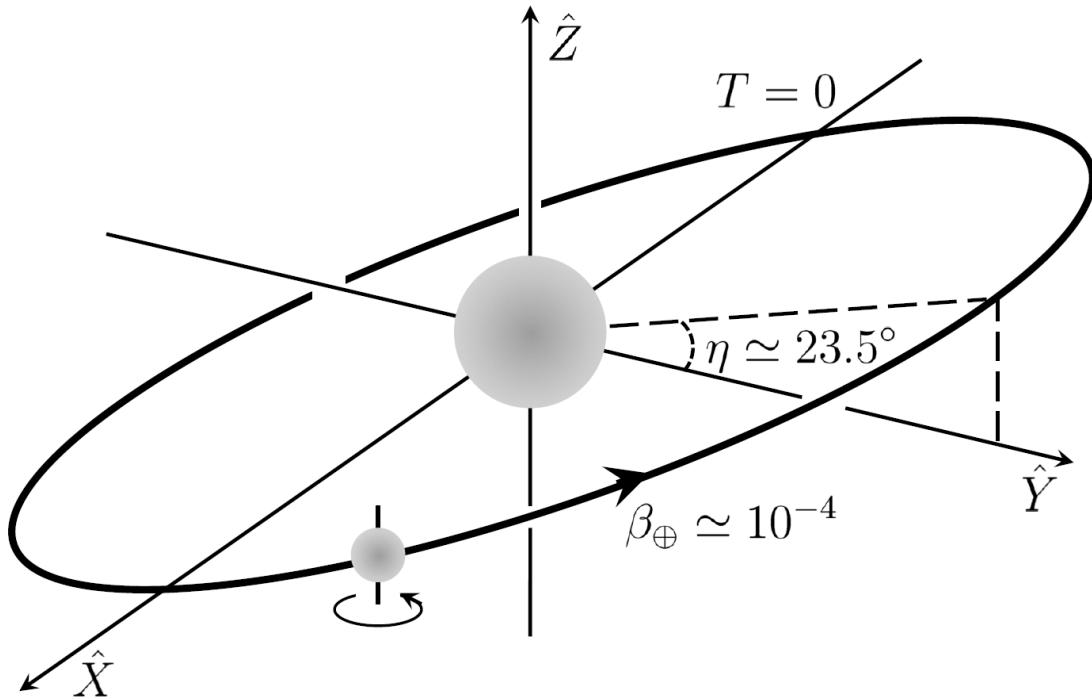
In the SM:



Effective Hamiltonian  $\Delta S=1$  non-leptonic

$$\mathcal{H} \sim \frac{4G_F}{2\sqrt{2}} \cos \theta_C \sin \theta_C \sum_{i=1}^6 c_i \mathcal{O}_i,$$

# How to test Lorentz violation?

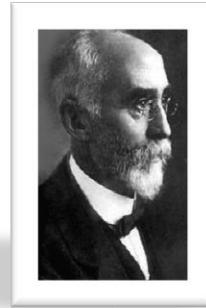


Sun-centered reference frame

# Testing Lorentz violation

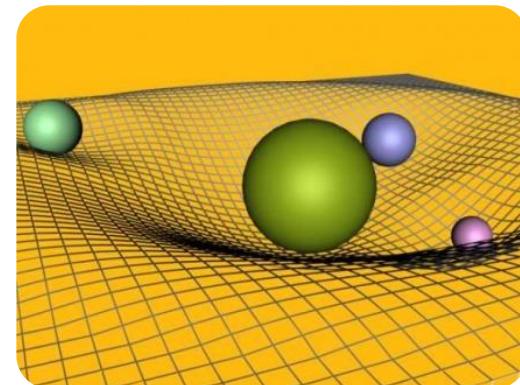
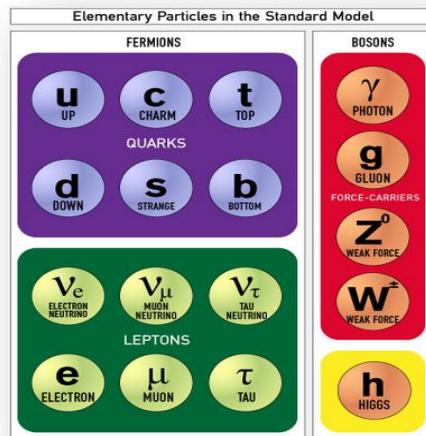


Lorentz  
invariance



CPT

Charge conjugation  
Parity  
Time-reversal



$\chi_{\mu\nu}$	Decay	Experiment
$\chi_{r,S}^{lk} < 10^{-7}$	Forbidden $\beta$ -decay	Newman
$\tilde{\chi}_i^l < 10^{-3}$	Allowed $\beta$ -decay	KVI Groningen
$\chi_{r,S}^{0l} < 10^{-3}$	$K_S$ tree-model	KLOE

# Status of constraints – slide H.W.

- Assuming contribution of only one element (others are put at zero)

- $|\chi_{rs}^{\mu\nu}| < \begin{bmatrix} 10^{-6} & 10^{-7} & 10^{-6} & 10^{-7} \\ 10^{-7} & 10^{-6} & 10^{-7} & 10^{-6} \\ 10^{-7} & 10^{-6} & 10^{-7} & 10^{-6} \\ 10^{-8} & 10^{-6} & 10^{-8} & 10^{-6} \end{bmatrix}$  and  $|\chi_{ia}^{\mu\nu}| < \begin{bmatrix} \times & - & - & - \\ - & \times & 10^{-8} & 10^{-7} \\ - & 10^{-8} & \times & 10^{-7} \\ - & 10^{-7} & 10^{-7} & \times \end{bmatrix}$

- All elements free (cancellations may occur)

- $|\chi_{rs}^{\mu\nu}| < \begin{bmatrix} 10^{-5} & 10^{-4} & 10^{-4} & 10^{-2} \\ 10^{-4} & - & 10^{-6} & 10^{-6} \\ 10^{-4} & 10^{-6} & - & 10^{-6} \\ 10^{-2} & 10^{-6} & 10^{-6} & 10^{-5} \end{bmatrix}$  and  $|\chi_{ia}^{\mu\nu}| < \begin{bmatrix} \times & - & - & - \\ - & \times & 10^{-2} & 10^{-2} \\ - & 10^{-2} & \times & 10^{-3} \\ - & 10^{-2} & 10^{-3} & \times \end{bmatrix}$

Forbidden  $\beta$  decay, this experiment, Kaon decay (penguin factor)

- Connection with SM extensions parameters (Kostelecky) (CPT even)

$$\chi_{rs}^{\mu\nu} = -(k_{\phi\phi}^S)^{\mu\nu} \text{ and } \chi_{ia}^{\mu\nu} = -(k_{\phi\phi}^A)^{\mu\nu} - k_{\phi W}^{\mu\nu}/2g$$